Maths — No Problem!

Calculation Policy

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Introduction

Maths — No Problem! materials use real-world contexts to help pupils understand the importance of mathematics in their everyday lives.

The progression of calculation skills, focusing on addition, subtraction, multiplication and division is developed using a Concrete Pictorial Abstract (CPA) approach and delivered through problem solving.

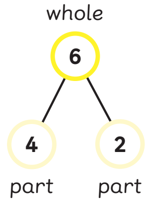
Key mathematical ideas are reinforced using Bruner's spiral curriculum: a teaching approach in which each subject or skill area is revisited in intervals at a more sophisticated level each time.

The **Maths — No Problem!** Calculation Policy guides practitioners through a clear progression of key skills and representations at each year group.

Addition Calculation Policy

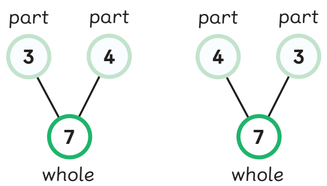
Year 1

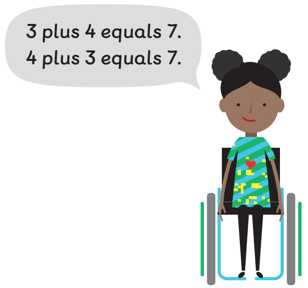
Year	Topic/Strand	Representation	Key Idea
Year 1	Part – Part – Whole	see below	This is a mathematical structure that underpins all addition situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 1	Number Bonds to 10	see below	Pupils develop automatic recall of number bonds to 10. This can be shown using a ten frame, a number bond diagram and written as an equation. This understanding can be related to adding tens, hundreds and so on when used with a sound understanding of place value.

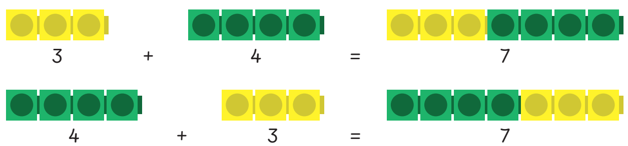


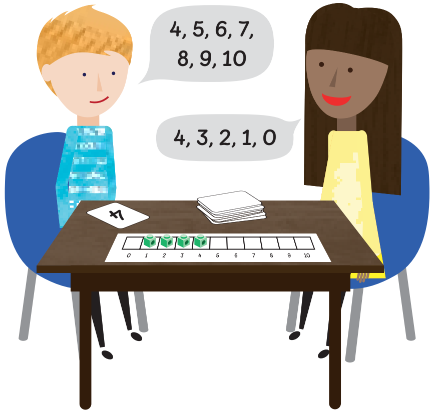
Number Bonds to 10 – Representation:

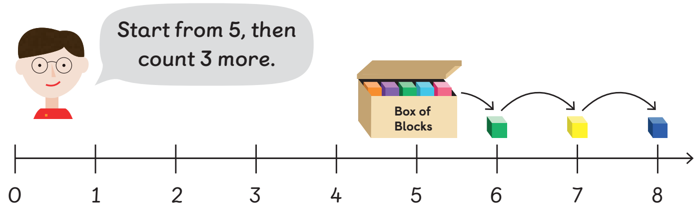
+	0	1	2	3	4	5	6	7	8	9	10
0	0 + 0	0 + 1	0 + 2	0 + 3	0 + 4	0 + 5	0 + 6	0 + 7	0 + 8	0 + 9	0 + 10
1	1 + 0	1 + 1	1 + 2	1 + 3	1 + 4	1 + 5	1 + 6	1 + 7	1 + 8	1 + 9	
2	2 + 0	2 + 1	2 + 2	2 + 3	2 + 4	2 + 5	2 + 6	2 + 7	2 + 8		
3	3 + 0	3 + 1	3 + 2	3 + 3	3 + 4	3 + 5	3 + 6	3 + 7			
4	4 + 0	4 + 1	4 + 2	4 + 3	4 + 4	4 + 5	4 + 6				
5	5 + 0	5 + 1	5 + 2	5 + 3	5 + 4	5 + 5					
6	6 + 0	6 + 1	6 + 2	6 + 3	6 + 4						
7	7 + 0	7 + 1	7 + 2	7 + 3							
8	8 + 0	8 + 1	8 + 2								
9	9 + 0	9 + 1									
10	10 + 0										

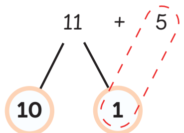






<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 1</td><td>Using a
Number Track</td><td>
</td><td>Pupils are first introduced to a linear number system through the number track. This is a precursor to the number line.

Pupils may benefit from placing items on the number track as they count and add, before moving on to use the more abstract number line.</td></tr>
<tr><td>Year 1</td><td>Counting
on Using a
Number Line</td><td>5 + 3 = $\boxed{\quad}$

</td><td>Pupils move from a number track to a number line, starting from zero and having marked increments of 1.

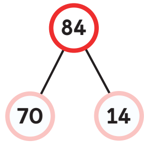
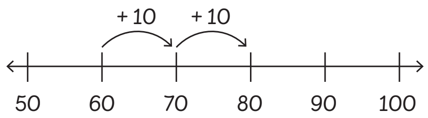
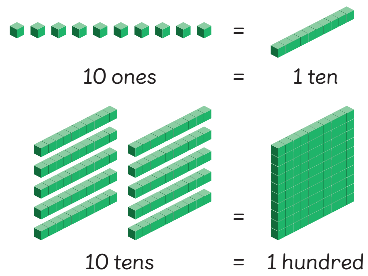
The use of the number line is further developed when counting starts from a given number, relying on pupils' ability to locate and count on from a given number.</td></tr>
<tr><td>Year 1</td><td>Adding by
Making 10</td><td>

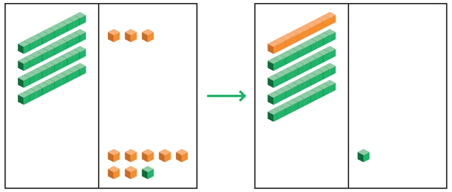
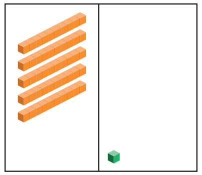
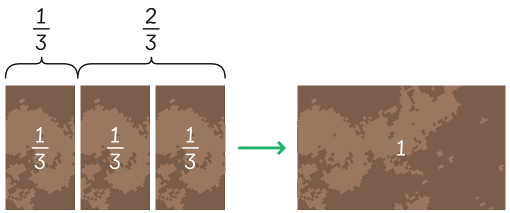
10 + 6 = 16
11 + 5 = 16</td><td>Pupils use their part–whole understanding to rename a number into its component parts in order to make 10 within an equation.

Pupils also look for combinations of numbers that make 10 in addition examples that have 3 numbers with a sum greater than 10.</td></tr>
</table>

Year	Topic/Strand	Representation	Key Idea
Year 1	Addition Word Problems	Emma has two balls. Sam has four balls. How many balls in total? + =	Pupils apply their knowledge of addition within the context of word problems. The problems may involve different situations, contexts or strategies.

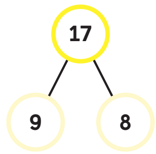
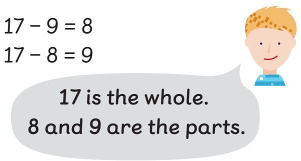
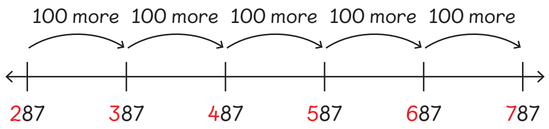
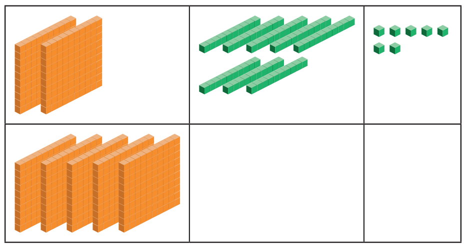
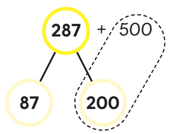
Addition Calculation Policy
Year 2

Year	Topic/Strand	Representation	Key Idea
Year 2	Part – Part – Whole	84 = 70 + 14 	This is a mathematical structure that underpins all addition situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 2	Counting on Using a Number Line	 60 + 20 = 80	The use of the number line is further developed when counting starts from a given number, relying on pupils' ability to locate and count from a given number, including starting from a 2-digit number. Initially a 1-digit number is added to a 2-digit number, then this progresses to a number line shown with intervals of 10 when adding 2-digit numbers that do not have any ones.
Year 2	Base 10 Blocks		The use of base 10 blocks provides a representation of the place value, primarily of 2-digit numbers. This representation is related to the formal written method but also encourages pupils to use their understanding of adding the same noun to add 2-digit numbers. For example, 20 + 30 can be understood as 2 tens + 3 tens. The sum of these numbers is 50 or 5 tens. An understanding of place value will support addition as well as subtraction, multiplication and division.

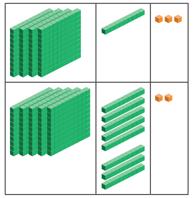
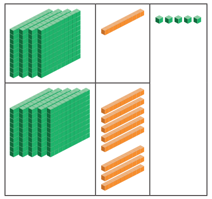
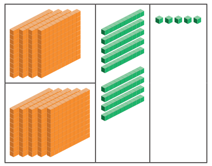
Year	Topic/Strand	Representation	Key Idea
Year 2	Formal Written Method	43 + 8 =  3 ones + 8 ones = 11 ones 11 ones = 1 ten and 1 one  tens ones 4 3 + 8 1 1   tens ones 4 3 + 8 1 1 + 4 0 5 1  4 tens + 1 ten = 5 tens 40 + 10 = 50 43 + 8 = 51 There are 51 bottles of water in total.	This is a procedural method that relies on a pupil's conceptual understanding of addition. This begins without renaming and progresses to the renaming of 10 ones into 1 ten. Pupils understand that at this stage, they start with the addition of the ones before they add the tens. This method is supported with base 10 block representation. The formal written method is always accompanied by a written equation to ensure that the relationship between the representations is made.
Year 2	Adding Fractions	 $\frac{1}{}$ and $\frac{2}{}$ make 1 whole.	Pupils use their understanding of adding the same noun when adding fractions through a written sentence. Fractions with the same denominator are added using a '[ ] and [ ] make [ ]' structure.

Addition Calculation Policy

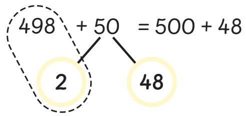
Year 3

Year	Topic/Strand	Representation	Key Idea
Year 3	Part – Part – Whole	 9 + 8 = 17 8 + 9 = 17 17 – 9 = 8 17 – 8 = 9 	This is a mathematical structure that underpins all addition situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 3	Counting on Using a Number Line	 287 + 500 = 787	The use of the number line is further developed when counting starts from a given number, relying on pupils' ability to locate and count from a given number, including starting from a 3-digit number. Initially a 1-digit number is added to a 3-digit number, then this progresses to a number line shown with intervals of 1, then 10 and eventually to 100.
Year 3	Base 10 Blocks	 287 + 500 = 787 787 fans watched the game in total.  h t o 2 8 7 + 5 0 0 7 8 7 200 + 500 = 700 87 + 700 = 787	The use of base 10 blocks provides a representation of the place value of 3-digit numbers. This representation is related to the formal written method but also encourages pupils to use their understanding of adding the same noun to add 3-digit numbers. For example, 200 + 500 can be understood as 2 hundreds + 5 hundreds. The sum of these numbers is 700 or 7 hundreds. Progression is made by adding ones, then tens and finally hundreds before the addition of all 3 is undertaken. An understanding of place value will support addition as well as subtraction, multiplication and division.

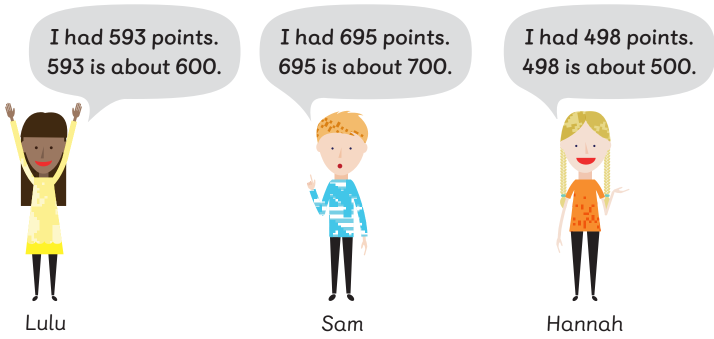
<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 3</td><td>Formal Written Method</td><td>413 + 582 =

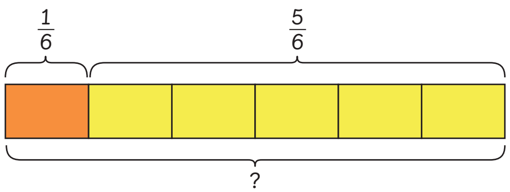
Step 1 Add the ones.
3 ones + 2 ones = 5 ones

<table><tr><th></th><th>h</th><th>t</th><th>o</th></tr><tr><td></td><td>4</td><td>1</td><td>3</td></tr><tr><td>+</td><td>5</td><td>8</td><td>2</td></tr><tr><td></td><td></td><td></td><td>5</td></tr></table>
Step 2 Add the tens.
1 ten + 8 tens = 9 tens

<table><tr><th></th><th>h</th><th>t</th><th>o</th></tr><tr><td></td><td>4</td><td>1</td><td>3</td></tr><tr><td>+</td><td>5</td><td>8</td><td>2</td></tr><tr><td></td><td></td><td>9</td><td>5</td></tr></table>
Step 3 Add the hundreds.
4 hundreds + 5 hundreds = 9 hundreds

<table><tr><th></th><th>h</th><th>t</th><th>o</th></tr><tr><td></td><td>4</td><td>1</td><td>3</td></tr><tr><td>+</td><td>5</td><td>8</td><td>2</td></tr><tr><td></td><td>9</td><td>9</td><td>5</td></tr></table>
413 + 582 = 995</td><td>This procedural method progresses from the renaming of 10 ones into 1 ten to include the renaming of 10 tens to 1 hundred. The procedure remains unchanged from Year 2.

Pupils understand that at this stage, they start with the addition of the ones, then the tens, then finally the hundreds.

This method is supported with base 10 block representation. The formal written method is always accompanied by a written equation to ensure that the relationship between the representations is made.</td></tr>
<tr><td>Year 3</td><td>Adding by Making 100</td><td>498 + 50 =

</td><td>Pupils are given the opportunity to further develop their number sense by using a ‘make 100’ strategy with numbers that are ‘near hundreds’.

They use their part–whole understanding to rename a given number to make 100. For example, 498 + 50 can be renamed as 498 + 2 + 48. Pupils add 2 to 498 to make 500, then add the remaining 48.</td></tr>
</table>

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 3</td><td>Estimating</td><td>


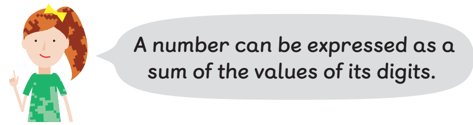
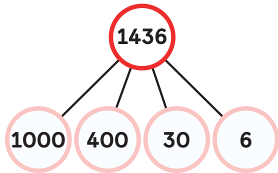
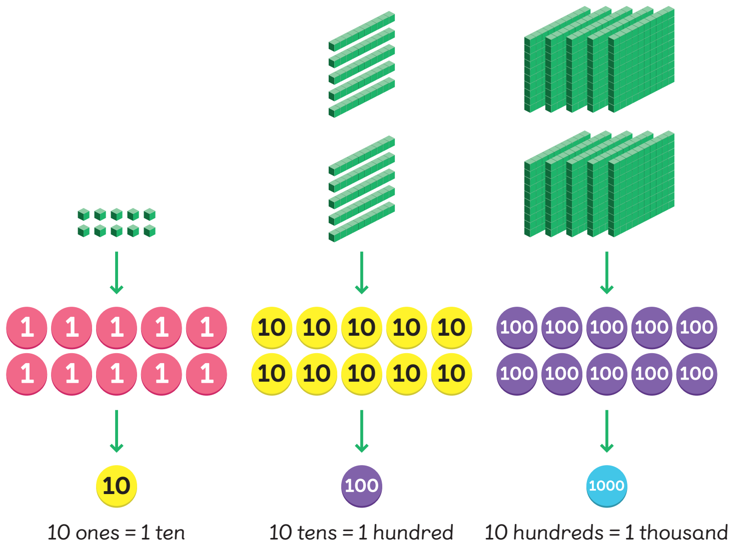
600 + 50 = 650
700 + 70 = 770
500 + 50 = 550
</td><td>Pupils use their number sense to recognise numbers close to a hundred and how estimation can help accuracy in completing a precise calculation.</td></tr>
<tr><td>Year 3</td><td>Adding Fractions</td><td>


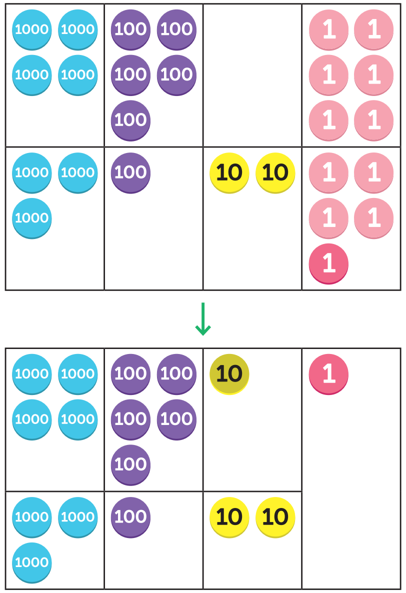
1 sixth and 5 sixths make 6 sixths.
$\frac{1}{6} + \frac{5}{6} = \frac{6}{6}$
$= 1$
</td><td>Pupils use their understanding of adding the same noun when adding fractions with the same denominator.

The adding of fractions uses equations and is supported through pictorial representation.</td></tr>
</table>

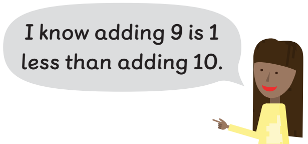
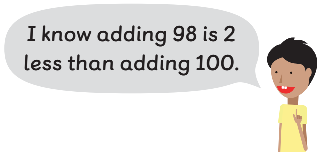
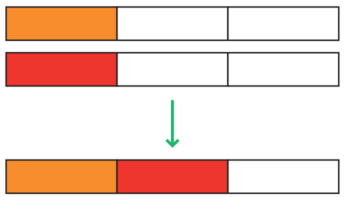
Addition Calculation Policy

Year 4

Year	Topic/Strand	Representation	Key Idea
Year 4	Part – Part – Whole	 1436 = 1000 + 400 + 30 + 6 	This is a mathematical structure that underpins all addition situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. The bar model is used as a representation of a problem that can be related to a part–whole addition situation. Pupils develop an understanding of the parts and the whole within an equation.
Year 4	Base 10 Blocks		The use of base 10 blocks provides a representation of the place value of 3-digit numbers. This representation is related to the formal written method but also encourages pupils to use their understanding of adding the same noun. In Year 4, a transition between base 10 blocks and place–value counters takes place.

Year	Topic/Strand	Representation	Key Idea
Year 4	**Place–Value Counters**	*4506 + 3125 =* *Step 1 Add the ones.* *6 ones and 5 ones = 11 ones* *Rename the ones.* *11 ones = 1 ten and 1 one*  $\begin{array}{cccc} & 4 & 5 & {}^{1}0 & 6 \\ + & 3 & 1 & 2 & 5 \\ \hline & & & & 1 \\ \hline \end{array}$	Place–value counters are used to represent addition situations. This transition relies on pupils understanding the value of each counter without being able to count its physical attributes. Pupils will have the opportunity to rename 10 counters of the same value to 1 counter with a value 10 times greater and vice versa. The idea of composing and decomposing at a rate of 10 should be well understood at this stage.

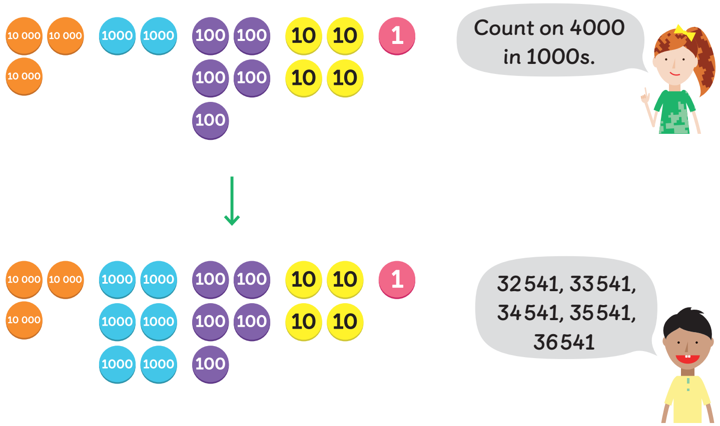
Year	Topic/Strand	Representation	Key Idea
Year 4	**Formal Written Method**	4188 + 3245 = $\begin{array}{rrrrrl} & 4 & 1 & 8 & 8 & \\ + & 3 & 2 & 4 & 5 & \\ \hline & & & 1 & 3 & \text{Add the ones.} \\ & & 1 & 2 & 0 & \text{Add the tens.} \\ & & 3 & 0 & 0 & \text{Add the hundreds.} \\ + & 7 & 0 & 0 & 0 & \text{Add the thousands.} \\ \hline & 7 & 4 & 3 & 3 & \\ \hline \end{array}$ $\begin{array}{rrrrr} & 2 & 6 & 1 & 2 \\ + & 4 & 2 & 6 & 4 \\ \hline & 6 & 8 & 7 & 6 \\ \hline \end{array}$	Pupils will have the opportunity to use a long and short version of this procedural method. In the long representation, the sum of adding each place is shown in its entirety before being added to find the final sum. In the short representation, the sum of each place is shown as part of the total sum and as a small number added to an existing place when a ten of one place is made. The procedure remains unchanged from Year 2.
Year 4	**Estimating the Sum**	Start by estimating. 4188 ≈ 4200 3245 ≈ 3200 4200 + 3200 = 7400 	Estimation is introduced as an approach to start a calculation. Estimation is a skill that helps develop number sense. Pupils are expected to be able to decide if an answer is reasonable. Beginning a calculation with estimation is developed during the addition chapter.
Year 4	**Making 10 and Making 100**	make 10 4072 + 8 = 4072 + 8 = 4070 + 10 4072 + 8 = 4080 make 100 97 + 5213 = 97 + 5213 = 100 + 5210 = 5310	A mental method that involves renaming numbers to make 10 or 100 before finding the sum. Pupils develop their number sense by recognising numbers close to a ten or close to a hundred and renaming a number in the equation to bring a number to the nearest 10 or nearest 100 without having to compensate the sum.

Year	Topic/Strand	Representation	Key Idea
Year 4	Adding Using Compensation	**1** Lulu used this method to find the sum of 3067 and 9. 3067 + 10 = 3077 3067 + 9 = 3076 1 less  **2** Ravi used this method to find the sum of 98 and 5262. 100 + 5262 = 5362 98 + 5262 = 5360 2 less 	A mental method that uses a similar equation in which a number in the original calculation is shown to the nearest 10 or 100 before carrying out the calculation. This calculation is used to help find the sum of the original equation.
Year 4	Adding Fractions	 $\frac{1}{3} + \frac{1}{3} = \frac{2}{3}$	Pupils use their understanding of adding the same noun when adding fractions with the same denominator. The adding of fractions uses equations and is supported through pictorial representation. Pupils use their understanding of equivalence to ensure denominators are the same before carrying out the addition.

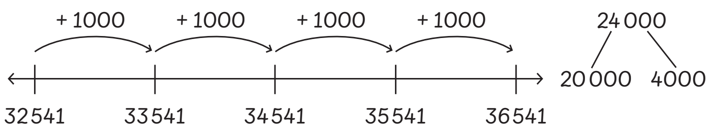
Addition Calculation Policy

Year 5

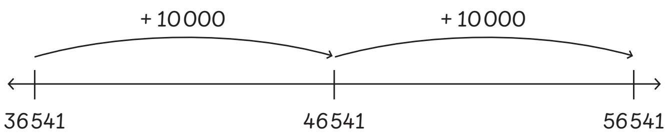
<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr>
<td>Year 5</td>
<td>Counting on Using Place–Value Counters</td>
<td>
32 541 + 24 000 =



</td>
<td>Pupils use place–value counters to support counting on in thousands to find the sum.</td>
</tr>
<tr>
<td>Year 5</td>
<td>Counting on Using Number Lines</td>
<td>
Count on 24 000 from 32 541.

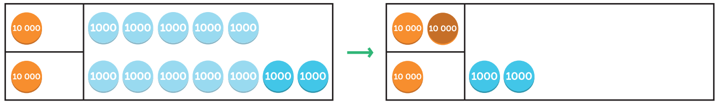
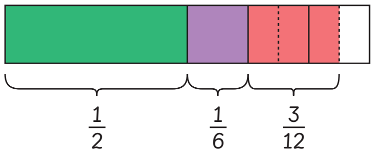


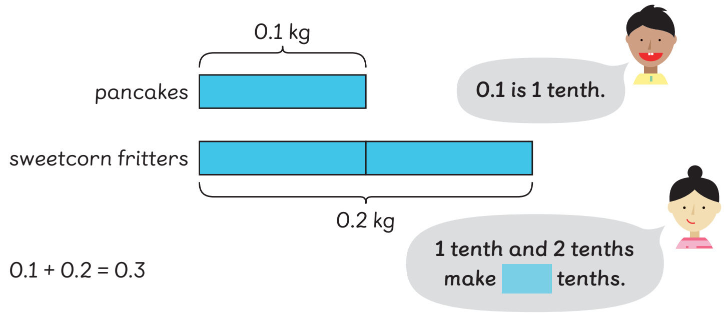
32 541 + 4000 = 36 541



36 541 + 20 000 = 56 541

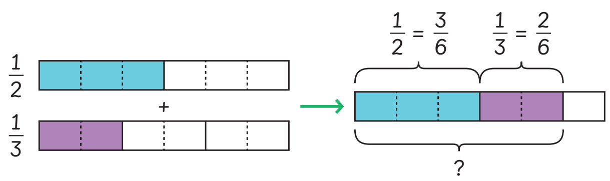
32 541 + 24 000 = 56 541
</td>
<td>Pupils count in thousands and ten thousands, using a number line to show this counting on method.</td>
</tr>
</table>

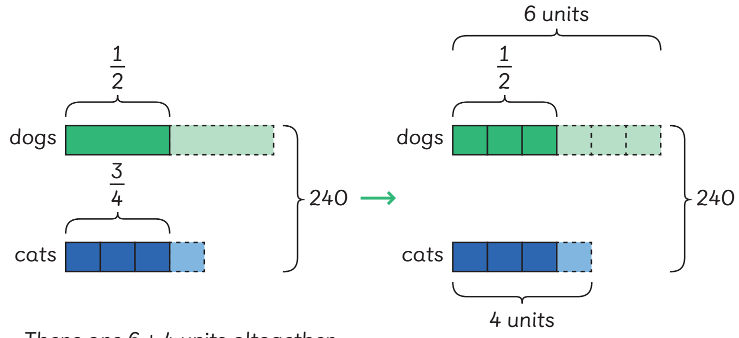
Year	Topic/Strand	Representation	Key Idea
Year 5	**Formal Written Method**	 $\begin{array}{r} {}^{1} \\ 15\ 000 \\ +\ 17\ 000 \\ \hline 32\ 000 \\ \hline \end{array}$ 5 thousands + 7 thousands = 12 thousands 12 thousands = 1 ten thousand + 2 thousands  15 000 + 17 000 = 32 000	Place–value counters are used to represent the formal written method. The procedure remains unchanged from Year 2.
Year 5	**Adding Fractions**	Add $\frac{1}{2}$, $\frac{1}{6}$ and $\frac{3}{12}$.  $\frac{1}{2} + \frac{1}{6} + \frac{3}{12} = \frac{6}{12} + \frac{2}{12} + \frac{3}{12}$ $= \frac{11}{12}$	Pupils use their understanding of adding the same noun when adding fractions with the same denominator. The adding of fractions uses equations and is supported through pictorial representation. Pupils use their understanding of equivalence to ensure denominators are the same before carrying out the addition.

Year	Topic/Strand	Representation	Key Idea
Year 5	**Adding Decimals**	 0.1 + 0.2 = 0.3	Pupils use their understanding of adding the same nouns when adding tenths. Tenths are represented using bar models, written words and equations.
Year 5	**Adding Decimals Using the Formal Written Method**	$\begin{array}{r} £\,{}^{1}1\,.\,8\,0 \\ +\,£\,0\,.\,7\,0 \\ \hline £\,2\,.\,5\,0 \\ \hline \end{array}$	The procedure for adding decimals using a formal written method is the same as when adding whole numbers, but attention needs to be given to the decimal point. The decimal point does not represent a place but separates the whole from the fractional part of a number. Careful alignment is needed when adding decimal numbers using a formal written method.

Addition Calculation Policy

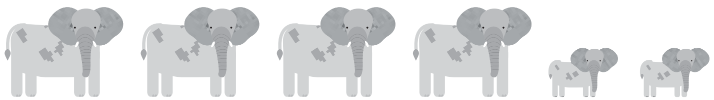
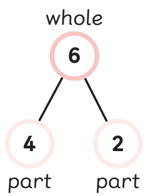
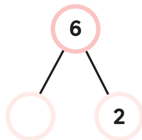
Year 6

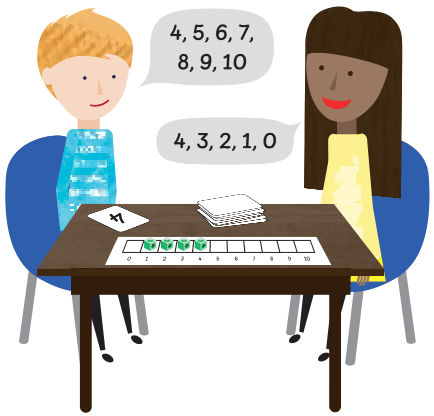
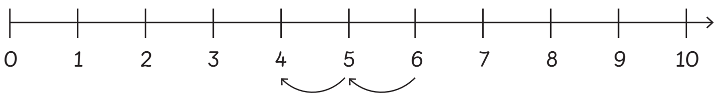
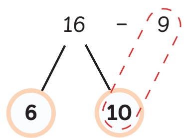
Year	Topic/Strand	Representation	Key Idea
Year 6	**Addition within Order of Operations**	*First, carry out all the operations in ( ).* *Next, perform all the multiplication and division.* *Then, calculate all the addition and subtraction.* Calculate. (a) $(1 + 3) \times 5 - 7 = \boxed{}$ (b) $1 + (3 \times 5) - 7 = \boxed{}$ (c) $(1 + 3) \times (7 - 5) = \boxed{}$	Pupils utilise the previous addition skills within mixed operation equations. Addition is carried out after multiplication and division. If only addition and subtraction are present in an equation, pupils work from left to right.
Year 6	**Adding Fractions**	 $\frac{1}{2} + \frac{1}{3} = \frac{5}{6}$	Pupils use their understanding of adding the same noun when adding fractions with the same and different denominators. Pupils use their understanding of equivalence to ensure the nouns and the denominators are the same before the calculation is completed.
Year 6	**Adding Decimals**	$\begin{array}{rrrrr} & £ & {}^{1}3 & . & 9\;0 \\ + & £ & 2 & . & 5\;0 \\ \hline & £ & 6 & . & 4\;0 \\ \hline \end{array}$	Pupils use their understanding of adding the same nouns when adding decimal numbers. They use place–value knowledge and composing and decomposing at a rate of 10 when adding decimals. The procedure remains the same as adding whole numbers.

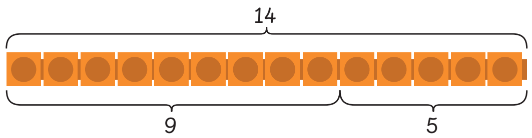
Year	Topic/Strand	Representation	Key Idea
Year 6	**Bar Models**	 *There are 6 + 4 units altogether.* 10 units = 240 1 unit = 24	Pupils are expected to utilise previously learned addition skills within increasingly complex situations. The procedure of addition is often at a level previously learned in isolation but the skill being developed is identifying when to use addition within a problem.

Subtraction Calculation Policy

Year 1

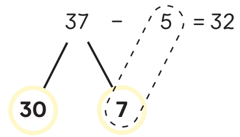
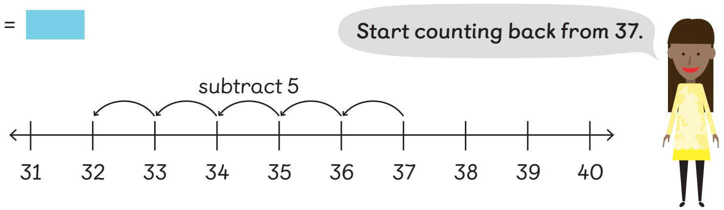
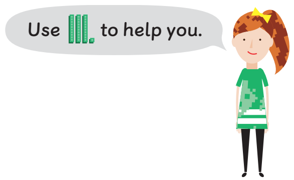
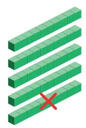
Year	Topic/Strand	Representation	Key Idea
Year 1	**Part–Part–Whole**	 6 – 4 = 2   2 elephants are not adults.	This is a mathematical structure that underpins subtraction situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 1	**Number Bonds to 10**	6 – 2 = ▭  	Pupils develop automatic recall of number bonds to 10. This can be shown using a ten frame, a number bond diagram and written as an equation. This understanding can be related to subtracting tens, hundreds and so on when used with a sound understanding of place value.

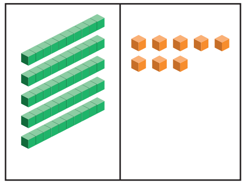
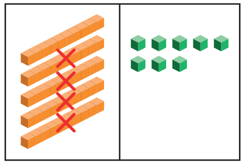
Year	Topic/Strand	Representation	Key Idea
Year 1	**Using a Number Track**		Pupils are first introduced to a linear number system through the number track. This is a precursor to the number line. Pupils may benefit from placing items on the number track as they count and subtract before moving on to use the more abstract number line.
Year 1	**Counting Back Using a Number Line**	 6 – 2 = 4	Pupils move from a number track to a number line, starting from zero and having marked increments of 1. The use of the number line is further developed when counting back starts from a given number, relying on pupils' ability to locate and count back from a given number.
Year 1	**Subtracting from 10**	 10 – 9 = 1 1 + 6 = 7 16 – 9 = 7 *There are 7 logs left.*	Pupils use their part–whole understanding to rename a number into its component parts in order to subtract from 10 within an equation.

Year	Topic/Strand	Representation	Key Idea
Year 1	**Subtraction Word Problems**	 14 – 9 = 5 *The number of people at the bus stop.* *The number of people who got on the bus.* *The number of people left at the bus stop.* *There are 5 people left at the bus stop.*	Pupils develop an understanding of situations and problems that require subtraction.

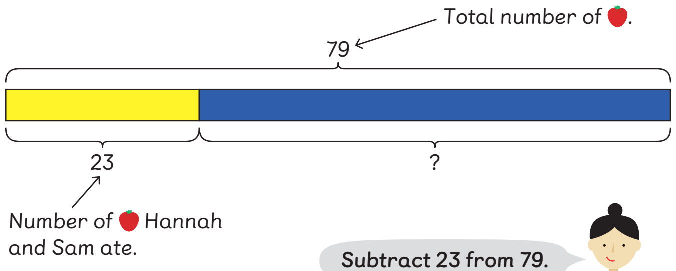
Subtraction Calculation Policy

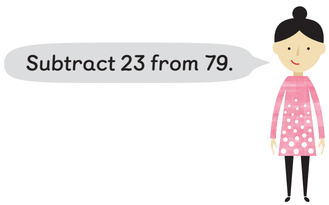
Year 2

Year	Topic/Strand	Representation	Key Idea
Year 2	Part–Part–Whole	 7 – 5 = 2 37 – 5 = 32	This is a mathematical structure that underpins subtraction situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 2	Counting Back Using a Number Line	37 – 5 =  37 – 5 = 32	The use of the number line is further developed when counting back starts from a given number, relying on pupils' ability to locate and count back from a given number, including starting from a 2-digit number. Initially a 1-digit number is subtracted from a 2-digit number, then this progresses to a number line shown with intervals of 10 when subtracting 2-digit numbers that do not have any ones.
Year 2	Base 10 Blocks	 *5 ones – 1 one = 4 ones* *5 – 1 = 4*   *5 tens – 1 ten = 4 tens* *50 – 10 = 40* 	The use of base 10 blocks provides a representation of the place value primarily of 2-digit numbers. This representation is related to the formal written method but also encourages pupils to use their understanding of subtracting the same noun to subtract 2-digit numbers. For example, 50 – 30 can be understood as 5 tens – 3 tens. The difference between the numbers is 20 or 2 tens. An understanding of place value will support subtraction as well as addition, multiplication and division.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr>
<td>Year 2</td>
<td>Formal Written Method</td>
<td>

<table>
<tr><th></th><th>tens</th><th>ones</th></tr>
<tr><td></td><td>5</td><td>8</td></tr>
<tr><td>–</td><td>4</td><td>0</td></tr>
<tr><td></td><td></td><td>8</td></tr>
</table>
8 ones – 0 ones = 8 ones
8 – 0 = 8

<table>
<tr><th></th><th>tens</th><th>ones</th></tr>
<tr><td></td><td>5</td><td>8</td></tr>
<tr><td>–</td><td>4</td><td>0</td></tr>
<tr><td></td><td>1</td><td>8</td></tr>
</table>
5 tens – 4 tens = 1 ten
50 – 40 = 10
58 – 40 = 18
</td>
<td>This is a procedural method that relies on a pupil's conceptual understanding of subtraction.

Initially, this begins without renaming and progresses to the renaming of 1 ten into 10 ones. Pupils understand that at this stage, they start with the subtraction of the ones before they subtract the tens. This method is supported with base 10 block representation.

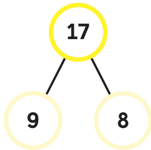
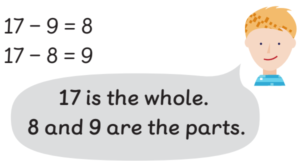
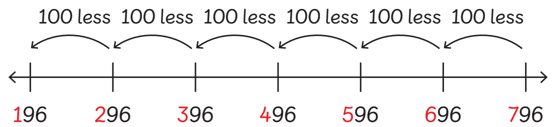
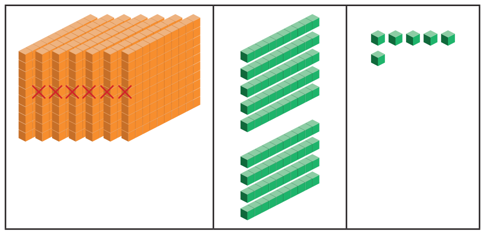
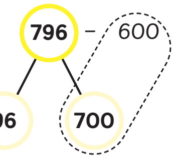
The formal written method is always accompanied by a written equation to ensure that the relationship between the representations are made.</td>
</tr>
<tr>
<td>Year 2</td>
<td>Subtraction Word Problems</td>
<td>


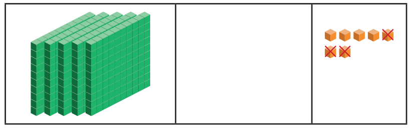
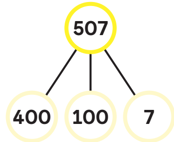
79 – 23 = 56
There are 56 strawberries left.


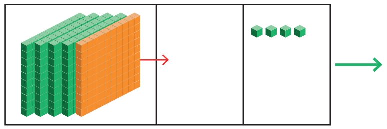
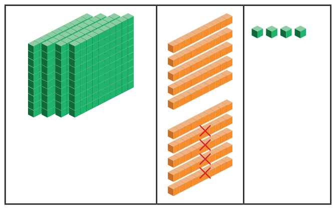
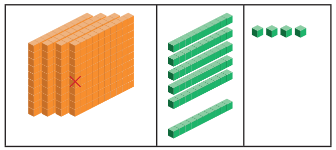
</td>
<td>Pupils develop an understanding of situations and problems that require subtraction.</td>
</tr>
</table>

Subtraction Calculation Policy

Year 3

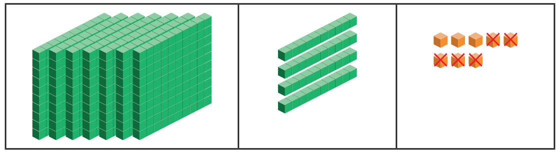
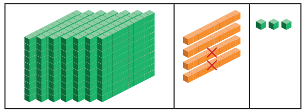
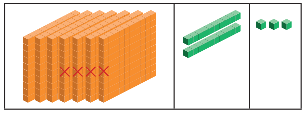
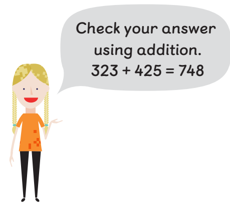
Year	Topic/Strand	Representation	Key Idea
Year 3	Part–Part–Whole	 9 + 8 = 17 8 + 9 = 17 17 − 9 = 8 17 − 8 = 9 	This is a mathematical structure that underpins subtraction situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 3	Counting Back Using a Number Line	 796 − 600 = 196	The use of the number line is further developed when counting back starts from a given number, relying on pupils' ability to locate and count back from a given number, including starting from a 3-digit number. Initially a 1-digit number is subtracted from a 3-digit number, then this progresses to a number line shown with intervals of 1, then 10 and then progressing to 100.
Year 3	Base 10 Blocks	 796 − 600 = 196 There were 196 people left at the airport.  h t o 7 9 6 − 6 0 0 1 9 6 700 − 600 = 100 96 + 100 = 196	The use of base 10 blocks provides a representation of the place value of 3-digit numbers. This representation is related to the formal written method but also encourages pupils to use their understanding of subtracting the same noun to subtract from 3-digit numbers. For example, 700 – 400 can be understood as 7 hundreds – 4 hundreds. The difference between these numbers is 300 or 3 hundreds. Progression is made by subtracting ones, then tens and finally hundreds before the subtraction of all 3 places is undertaken. An understanding of place value will support subtraction as well as addition, multiplication and division.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr>
<td>Year 3</td>
<td>Formal Written Method</td>
<td>
507 − 143 = $\boxed{}$
Step 1 Subtract the ones.

7 ones − 3 ones = 4 ones


$\begin{array}{cccc} & h & t & o \\ & 5 & 0 & 7 \\ - & 1 & 4 & 3 \\ \hline & & & 4 \\ \hline \end{array}$
Step 2 Rename 1 hundred as 10 tens.
Subtract the tens.


10 tens − 4 tens = 6 tens
$\begin{array}{cccc} & h & t & o \\ & \overset{4}{\cancel{5}} & \overset{10}{\cancel{0}} & 7 \\ - & 1 & 4 & 3 \\ \hline & & 6 & 4 \\ \hline \end{array}$
Step 3 Subtract the hundreds.

4 hundreds − 1 hundred = 3 hundreds
507 − 143 = 364
$\begin{array}{cccc} & h & t & o \\ & \overset{4}{\cancel{5}} & \overset{10}{\cancel{0}} & 7 \\ - & 1 & 4 & 3 \\ \hline & 3 & 6 & 4 \\ \hline \end{array}$
</td>
<td>
This procedural method progresses from the renaming of 10 ones into 1 ten to include the renaming of 10 tens to 1 hundred when necessary. The procedure itself remains unchanged from Year 2.

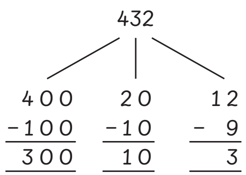
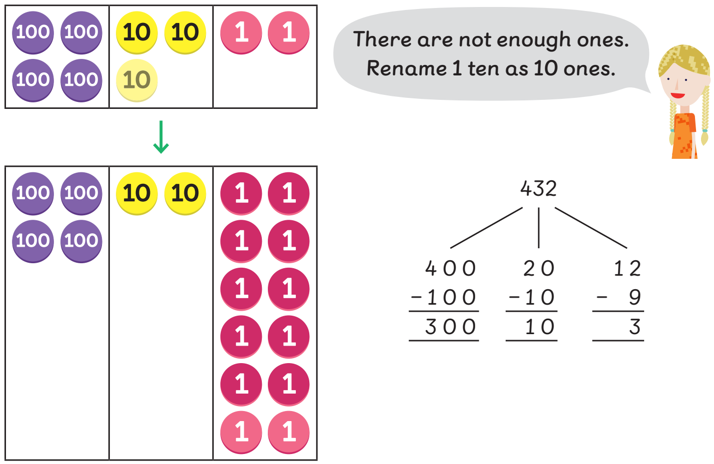
Pupils understand that at this stage, they start with the subtraction of the ones, then the tens, then finally the hundreds.

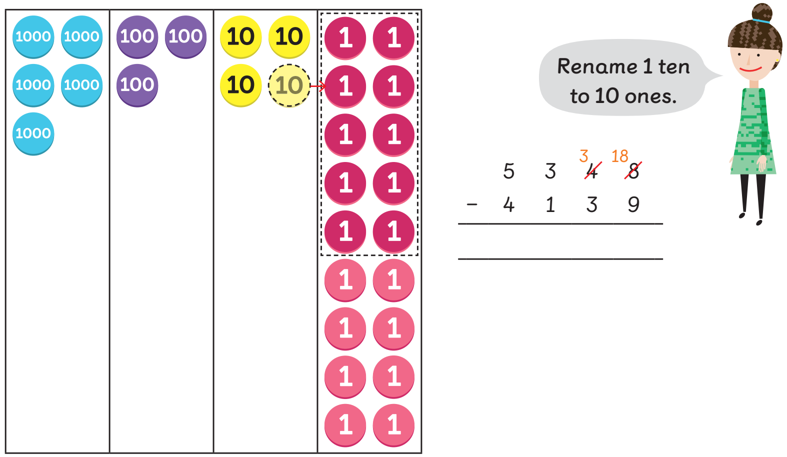
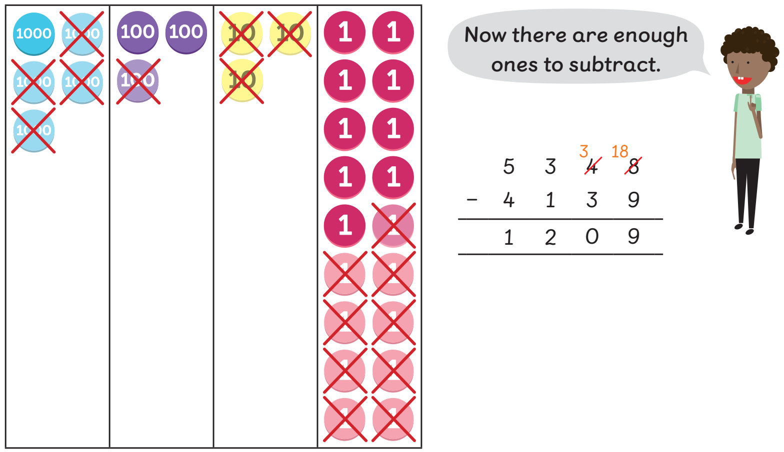
This method is supported with base 10 block representation. The formal written method is always accompanied by a written equation to ensure that the relationship between the representations are made.
</td>
</tr>
</table>

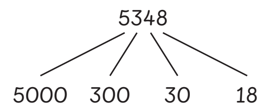
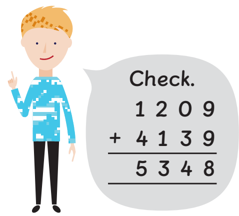
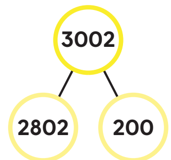
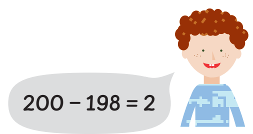
Year	Topic/Strand	Representation	Key Idea
Year 3	**Inverse Operation**	*748 − 425 = $\boxed{}$* *Step 1 Subtract the ones.* *8 ones − 5 ones = 3 ones*  $\begin{array}{cccc} & h & t & o \\ & 7 & 4 & 8 \\ - & 4 & 2 & 5 \\ \hline & & & 3 \\ \hline \end{array}$	Pupils should understand that subtraction is the inverse operation of addition. They are encouraged to check completed subtraction calculations using addition.
Year 3	**Difference Using a Bar Model**	*Step 2 Subtract the tens.* *4 tens − 2 tens = 2 tens*  $\begin{array}{cccc} & h & t & o \\ & 7 & 4 & 8 \\ - & 4 & 2 & 5 \\ \hline & & 2 & 3 \\ \hline \end{array}$ *Step 3 Subtract the hundreds.* *7 hundreds − 4 hundreds = 3 hundreds*  $\begin{array}{cccc} & h & t & o \\ & 7 & 4 & 8 \\ - & 4 & 2 & 5 \\ \hline & 3 & 2 & 3 \\ \hline \end{array}$ *748 − 425 = 323* *323 tomatoes are left.* 	Pupils are required to find the difference in a comparison problem when represented by a bar model. To find the difference, the known part is subtracted from the quantity it is being compared to. The comparison model reinforces the understanding of difference in subtraction.

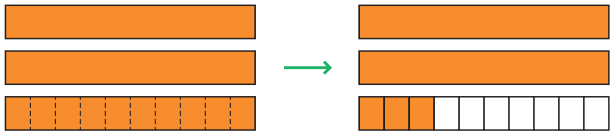
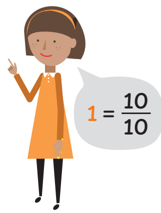
Subtraction Calculation Policy

Year 4

Year	Topic/Strand	Representation	Key Idea
Year 4	Part–Part–Whole		This is a mathematical structure that underpins subtraction situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.
Year 4	Place–Value Counters	*What is the difference between 432 and 119?* 	Place–value counters are used to represent subtraction situations. This transition from base 10 blocks relies on pupils understanding the value of each counter without being able to count its physical attributes. Pupils will have the opportunity to rename 1 counter to 10 counters with a value 10 times smaller in order to carry out a formal written method. The idea of decomposing at a rate of 10 should be well understood at this stage.

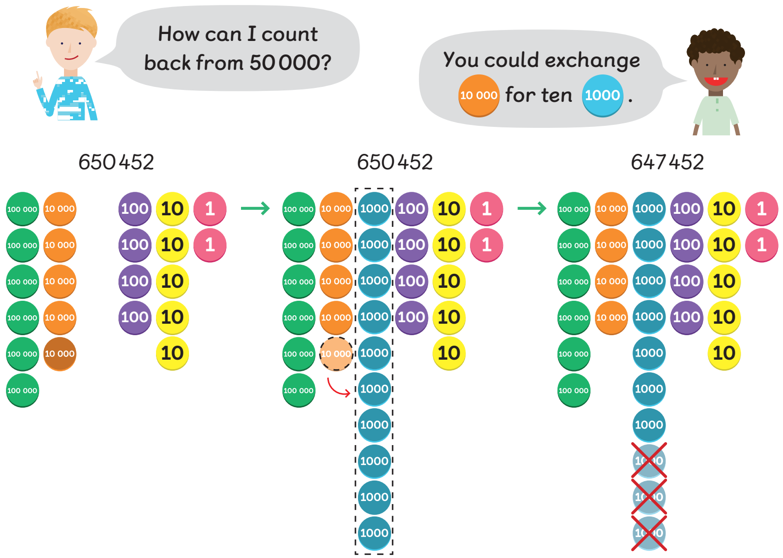
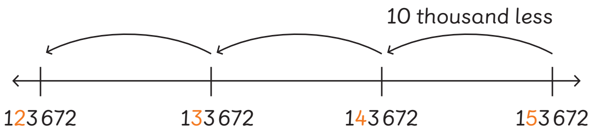
Year	Topic/Strand	Representation	Key Idea
Year 4	Formal Written Method	 	Pupils will use the formal written method initially without renaming, and then move to subtraction that requires renaming. The procedure remains the same as learned in Year 3 but the numbers increase to include 4-digit numbers being subtracted from 4-digit numbers.

Year	Topic/Strand	Representation	Key Idea
Year 4	**Using Addition to Check Subtraction**	 $\begin{array}{rrrrr} & 5 & 3 & \overset{3}{\cancel{4}} & \overset{18}{\cancel{8}} \\ - & 4 & 1 & 3 & 9 \\ \hline & 1 & 2 & 0 & 9 \\ \hline \end{array}$ *Step 1* *Subtract the ones.* *18 ones − 9 ones = 9 ones* *Step 2* *Subtract the tens.* *3 tens − 3 tens = 0 tens* *Step 3* *Subtract the hundreds.* *3 hundreds − 1 hundred = 2 hundreds* *Step 4* *Subtract the thousands.* *5 thousands − 4 thousands = 1 thousand* 5348 − 4139 = 1209  	Pupils are encouraged to check subtraction calculations by adding the parts (the subtrahend and the difference) to ensure the sum is equal to the whole (the minuend).
Year 4	**Mental Methods**	3002 − 198 = 2804  3002 − 198 = 2802 + 2  	Mental subtraction methods include partitioning the minuend to simplify the subtraction calculation. The approach shown is supported by an understanding of number bonds to 10 and to 100.

Year	Topic/Strand	Representation	Key Idea
Year 4	**Subtracting Fractions**	 $3 - \frac{7}{10} = 2\frac{10}{10} - \frac{7}{10}$ 2 1 $= 2\frac{3}{10}$  	Pupils use their understanding of subtracting the same nouns when subtracting fractions with the same denominator. The subtraction of fractions or finding the difference between fractions is supported through pictorial representation. Pupils use their understanding of equivalence to ensure denominators are the same before carrying out the subtractions.

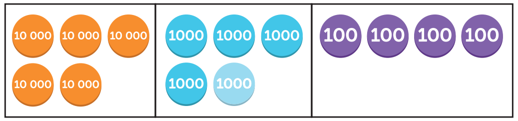
Subtraction Calculation Policy

Year 5

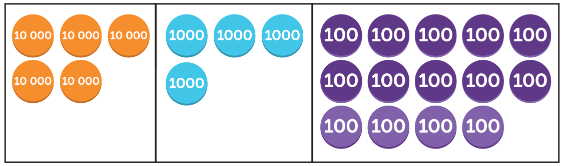
Year	Topic/Strand	Representation	Key Idea
Year 5	**Counting Back Using Place–Value Counters**	Subtract 3000 from 650 452. Start at 650 452. Count back in 1000s.  650 452 − 3000 =	Pupils use place–value counters to support counting back in thousands to find the difference.
Year 5	**Counting Back Using Number Lines**	Count back 30 000 from 153 672.  153 672 − 30 000 =	Pupils count back in thousands and ten thousands, using a number line to show this counting back method.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr>
<td>Year 5</td>
<td>Formal Written Method</td>
<td>

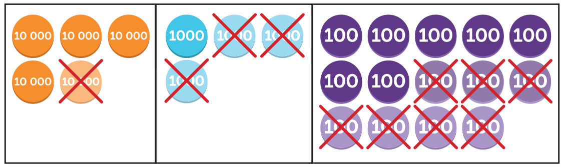
55 400 − 13 700 =



Rename 1 thousand as 10 hundreds.



Subtract 7 hundreds from 14 hundreds.



$$\begin{array}{rrrrr} & {}^{4} & {}^{14} & & \\ 5 & \cancel{5} & \cancel{4} & 0 & 0 \\ -\,1 & 3 & 7 & 0 & 0 \\ \hline & & 7 & 0 & 0 \end{array}$$

Subtract the thousands.

$$\begin{array}{rrrrr} & {}^{4} & {}^{14} & & \\ 5 & \cancel{5} & \cancel{4} & 0 & 0 \\ -\,1 & 3 & 7 & 0 & 0 \\ \hline & 1 & 7 & 0 & 0 \end{array}$$

Subtract the ten thousands.

$$\begin{array}{rrrrr} & {}^{4} & {}^{14} & & \\ 5 & \cancel{5} & \cancel{4} & 0 & 0 \\ -\,1 & 3 & 7 & 0 & 0 \\ \hline 4 & 1 & 7 & 0 & 0 \end{array}$$

</td>
<td>

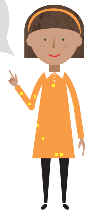
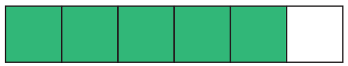
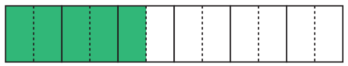
Place–value counters are used to represent the formal written method. The procedure to subtract using numbers up to 6-digits using the formal written method remains the same as when it was first introduced.

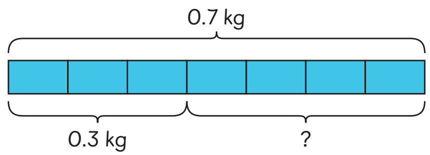
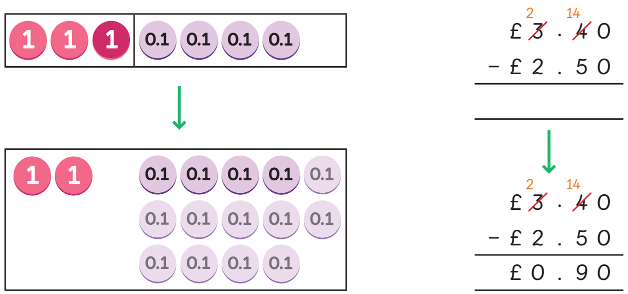
Pupils begin at the least value place and work to the left through the places to find the difference.

Renaming takes place when a calculation in a place cannot be done. Again, this procedure is the same as when this was first learned and requires the renaming of the minuend.

The renaming of the minuend is also represented using a number bond, providing the foundation for mental methods that require renaming.

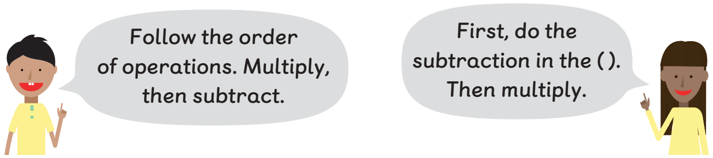
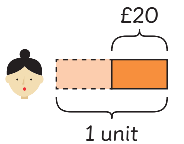
</td>
</tr>
</table>

Year	Topic/Strand	Representation	Key Idea
Year 5	**Checking by Using Estimation and Addition**	75 241 − 34 658 = 40 583 $\begin{array}{r} 40\,583 \\ +\ 34\,658 \\ \hline 75\,241 \\ \hline \end{array}$  $75\,241 - 34\,658 \approx 75\,000 - 35\,000$ $= 40\,000$ 	Pupils are encouraged to check the reasonableness of their answers by initially finding an estimated difference. When using estimation to check, pupils initially round to the nearest thousand before calculation. When using addition to check the difference, pupils add the difference and the subtrahend to check it is equal to the minuend.
Year 5	**Subtracting Fractions**	 $1 - \frac{1}{6} = \frac{6}{6} - \frac{1}{6}$ $= \frac{5}{6}$  $\frac{5}{6} - \frac{5}{12} = \frac{10}{12} - \frac{5}{12}$ $= \frac{5}{12}$ 	Pupils use their understanding of subtracting the same nouns when subtracting fractions with the same denominator. The subtraction of fractions or finding the difference between fractions is supported through pictorial representation. Pupils use their understanding of equivalence to ensure denominators are the same before carrying out the subtractions.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 5</td><td>Subtracting Decimals</td><td>Find the difference between 0.7 kg and 0.3 kg.

0.7 − 0.3 = 0.4</td><td>Pupils use their understanding of subtracting the same nouns when subtracting tenths. Tenths are represented using bar models, written words and equations.</td></tr>
<tr><td>Year 5</td><td>Subtracting Decimals Using the Formal Written Method</td><td>Find the difference between £3.40 and £2.50.
</td><td>The same procedure for subtracting decimals using a formal written method is the same as when subtracting whole numbers but attention needs to be given to the decimal point. The decimal point does not represent a place but separates the whole from the fractional part of a number. Careful alignment is needed when subtracting decimal numbers using a formal written method.</td></tr>
<tr><td>Year 5</td><td>Subtracting Decimals Using Equivalence</td><td></td><td>Pupils use their understanding of equivalence to subtract a decimal from a whole number. For example, when calculating 4 – 0.6 we can rename 4 as 40 tenths, so the calculation becomes 40 tenths – 6 tenths. Once the nouns are the same, the subtraction can be carried out. 40 tenths – 6 tenths = 34 tenths = 3.4</td></tr>
</table>

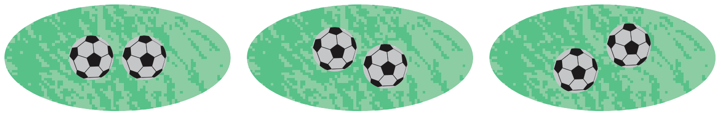
Subtraction Calculation Policy

Year 6

Year	Topic/Strand	Representation	Key Idea
Year 6	**Subtraction within Order of Operations**	*First, carry out all the operations in ( ).* *Next, perform all the multiplication and division.* *Then, calculate all the addition and subtraction.* $15 - 4 \times 3 = 15 - 12$ $= 3$ $(15 - 4) \times 3 = 11 \times 3$ $= 33$  	Pupils utilise the previous subtraction skills within mixed operation equations. Subtraction is carried out after multiplication and division. If only addition and subtraction are present in an equation, pupils work from left to right.
Year 6	**Bar Models**	  = £40 − £20 = £20	Pupils are expected to utilise previously learned subtraction skills within increasingly complex situations. The procedure of subtraction is often at a level previously learned in isolation but the skill being developed is identifying when to use subtraction within a problem.

Multiplication Calculation Policy

Year 1

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 1</td><td>Equal Groups</td><td>


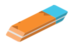
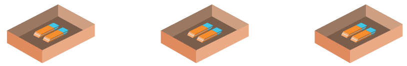
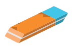
There are 2 ⚽ in each group.
Each group has an equal number of ⚽.
The balls are in equal groups.

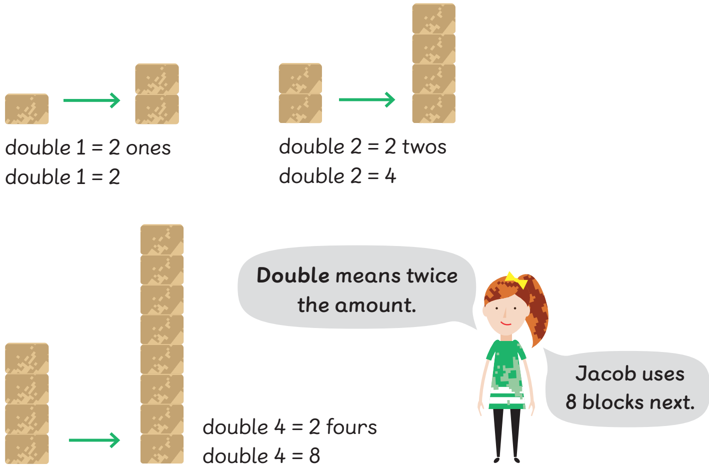
</td><td>
Pupils learn to recognise groups that are equal in quantity, initially using like items and then progressing to different items.

Pupils understand that equal groups can be represented by concrete items, diagrams and written numbers.

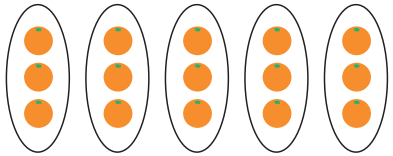
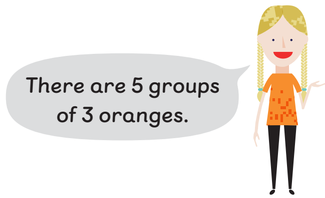
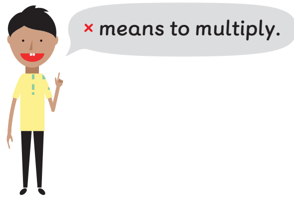
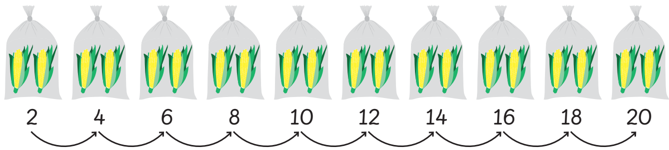
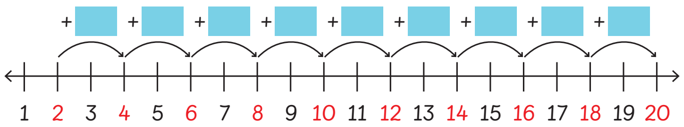
Pupils need to be secure in the abstraction principle of counting the quantity of items, regardless of the properties or characteristics of the items, in order to recognise equal groups in a range of situations.
</td></tr>
<tr><td>Year 1</td><td>Repeated Addition</td><td>

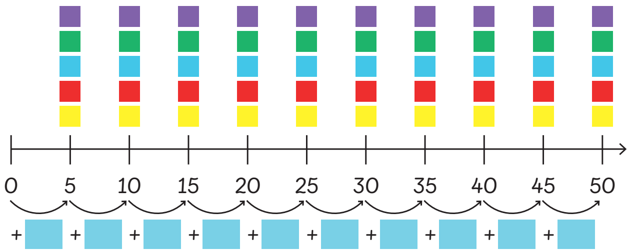
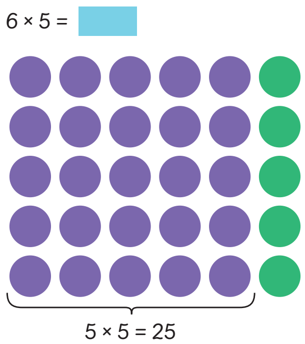
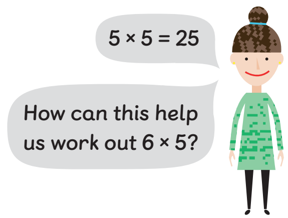
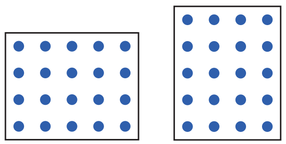
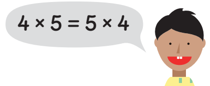

</td><td>
Initially, multiplication is shown as the addition of equal groups. The key idea of adding like nouns still applies in multiplication. A group of 3 bananas and 3 apples does not result in 6 bananas or 6 apples. In order to add, the nouns must be the same, in this case 6 pieces of fruit. This is also true of multiplication: 2 groups of 3 pieces of fruit makes 6 pieces of fruit.
</td></tr>
</table>

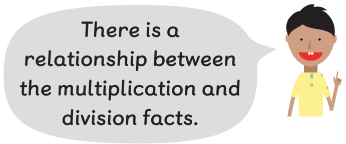
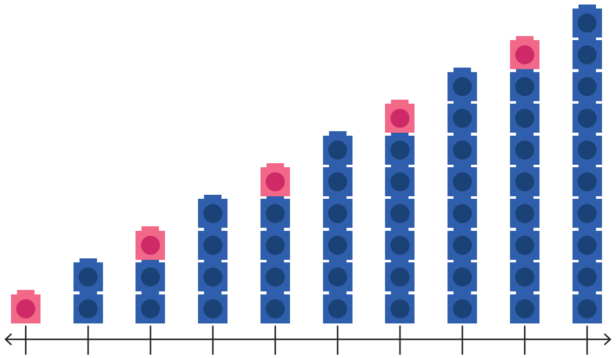
Year	Topic/Strand	Representation	Key Idea
Year 1	**Counting in 2s, 5s and 10s**	There are 3 groups of 2  .  2 2 2 3 groups of 2 = 6 3 twos = 6 There are 6  . 	Pupils start to count in multiples of 2 and multiples of 10, then progress to counting in multiples of 2, 5 and 10 supported by discrete, countable representations.
Year 1	Arrays	 3 rows of 5 3 fives = 15 There are 15 children altogether. 1 row of 5 = 5 2 rows of 5 = 10 3 rows of 5 = 	Multiplication is represented by arrays, beginning with making equal rows and further developing the language associated with arrays. For example: 'There are 3 rows of 5. There are 15 altogether.'

Year	Topic/Strand	Representation	Key Idea
Year 1	Doubles		The diagrams used to support learning how to double numbers, not only show equal groups of 2 being added each time, but also show the pattern scaling up and each 'tower' being twice the height of the tower just before it. Pupils can develop the language associated with multiplication by describing the growing block pattern. This also provides the basis for understanding halving, in which the representation scales down.

Multiplication Calculation Policy
Year 2

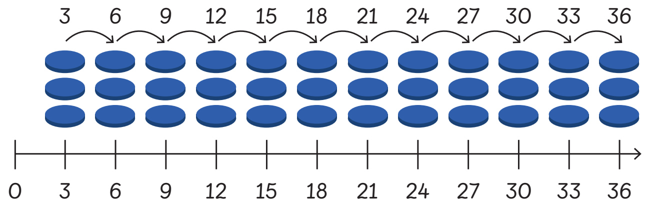
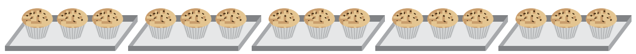
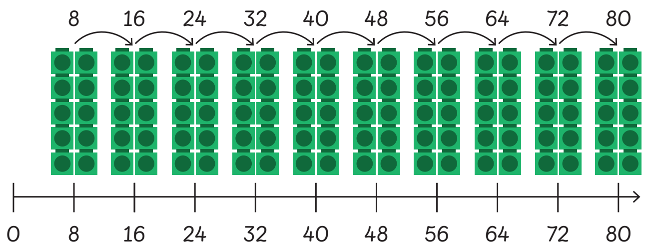
Year	Topic/Strand	Representation	Key Idea
Year 2	Equal Groups	 3 + 3 + 3 + 3 + 3 = 15  There are 15 oranges in total. 5 threes = 15 5 groups of 3 = 15 5 × 3 = 15 5 times 3 equals 15 We read 5 × 3 = 15 as 5 times 3 equals 15.  	Pupils learn to recognise groups that are equal in quantity, initially using like items and then progressing to different items. Pupils understand that equal groups can be represented by concrete items, diagrams and written numbers. In Year 2, the progression to multiplication from repeated addition is shown as 3 + 3 + 3 + 3 + 3 being equal to 5 groups of 3 and 5 groups of 3 being equal to 5 × 3. Pupils read 5 × 3 as 5 groups of 3.
Year 2	Counting in 2s, 5s and 10s	  	When a pupil knows that the size of a group is 2, 5 or 10 and the group size remains consistent, they can count in multiples of 2, 5 and 10 to find the product. Counting in multiples is supported by representation on a number line.

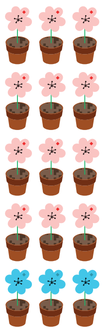
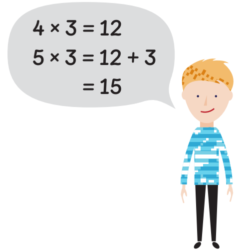
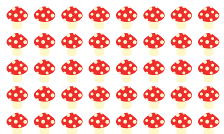
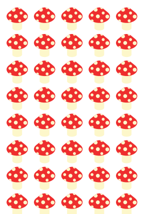
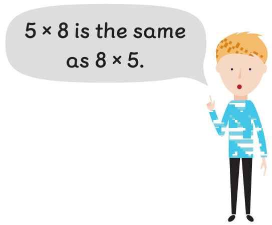
Year	Topic/Strand	Representation	Key Idea
Year 2	Number Line		Counting in multiples is shown on a number line. The increasingly abstract nature of the number line is shown as intervals change from 1 to 2, 5 and 10.
Year 2	Associated Facts	  $6 \times 5 = 25 + 5$ $= 30$	As pupils become more fluent and their understanding of their times tables increases, they are expected to use this knowledge to calculate associated facts. A pupil should be able to relate 10 × 5 to 9 × 5, knowing that the latter expression is 1 group of 5 less. So, 9 × 5 = 50 – 5.
Year 2	Commutativity	 $4 \times 5 = 20$ $5 \times 4 = 20$ 	Pupils learn that the order of the factors in an equation does not affect the product. This is supported pictorially through the use of arrays.

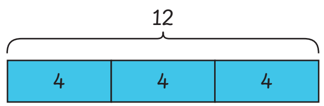
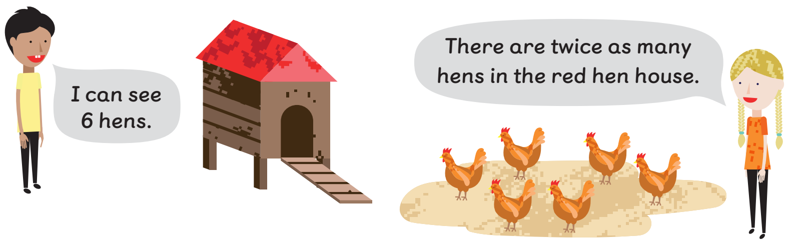
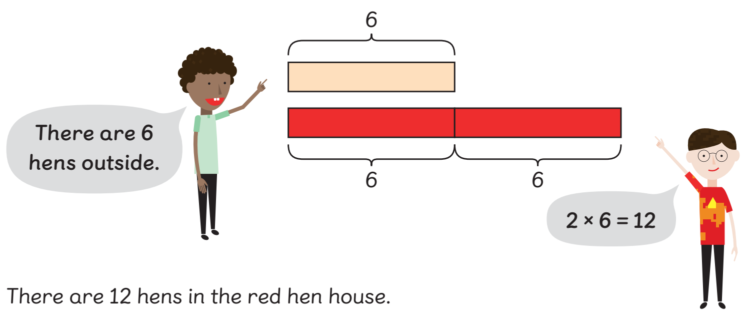
Year	Topic/Strand	Representation	Key Idea
Year 2	Fact Families	$10 \times 2 = 20$ $20 \div 2 = 10$ $2 \times 10 = 20$ $20 \div 10 = 2$  	Pupils relate multiplication and division and see the connection between them when completing fact families. Pupils develop an understanding that factor × factor = product and product ÷ factor = factor. Once the understanding of this is secure, pupils can relate this to both multiplication and division situations.
Year 2	Odd and Even Numbers	 	Pupils develop an understanding that even numbers can be put into groups of 2 exactly but when odd numbers are grouped in twos, there is always 1 remaining.

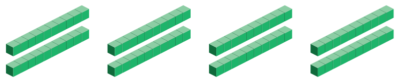
Multiplication Calculation Policy

Year 3

Year	Topic/Strand	Representation	Key Idea
Year 3	Counting in 3s, 4s and 8s		When a pupil knows that the size of a group is 3, 4 and 8 and the group size remains consistent, they can count in multiples of 3, 4 and 8 to find the product. Counting in multiples is supported by representation on a number line.
Year 3	Equal Groups		Multiplication by 3, 4 and 8 is shown initially using equal groups. Specific language is used to support these examples, in this case '4 groups of 3', and this is immediately followed by the equation 4 × 3. This forms the basis of using known facts to find unknown facts.
Year 3	Number Line		Counting in multiples is shown on a number line. Multiples of 3, 4 and 8 are used as the intervals on a number line to support skip counting using these multiples.

Year	Topic/Strand	Representation	Key Idea
Year 3	Associated Facts	 	Once the understanding of multiplication as the adding of equal groups is secure, this knowledge can be used to find unknown facts. For example, if a pupil knows 5 × 3 as 5 groups of 3, they can understand that 6 × 3 is simply 1 more group of 3. So, 6 × 3 = 15 + 3; 4 × 3 is seen as 1 group fewer than 5 × 3; 4 × 3 = 15 – 3. This structure is used in all multiplication tables.
Year 3	Number Patterns		Pupils count in multiples of 3, 4 or 8 to identify missing multiples in a sequence. This reinforces the products found within the 3, 4 and 8 times tables.
Year 3	Commutativity	 There are 5 rows of 8 mushrooms. 5 × 8 = 40  There are 8 rows of 5 mushrooms. 8 × 5 = 40  There are 40 mushrooms.	The representation of multiplication as an array is used to further develop the understanding of commutativity. Having first understood multiplication as [ ] groups of [ ], pupils develop an understanding that 5 × 3 can also be read as 5 multiplied 3 times. Pupils should have a firm understanding that the order the factors are multiplied in does not change the product.

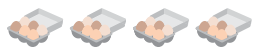
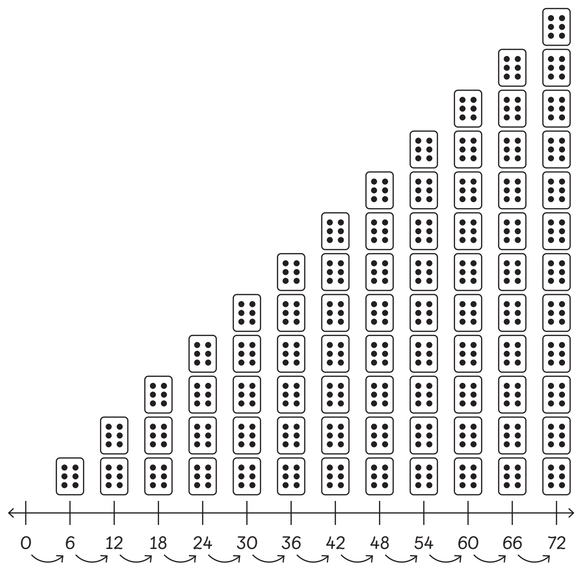
Year	Topic/Strand	Representation	Key Idea
Year 3	**Fact Families**	$12 \div 3 = 4$ $4 \times 3 = 12$ 	The relationship between multiplication and division is shown using fact families. The product is a result of multiplying factors and dividing the product by a factor will equal the factor used during multiplication.
Year 3	**Multiplication Using Bar Models**	 *How many hens are in the red hen house?*  *There are 12 hens in the red hen house.*	Bar models are used in multiplicative comparison problems. Pupils use multiplication skills to determine quantities in comparison to another quantity. Language such as ‘twice as many’, ‘three times as many’ and so on is developed in relation to multiplicative comparison problems.

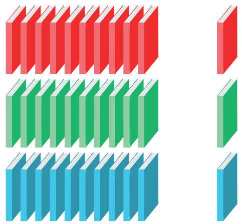
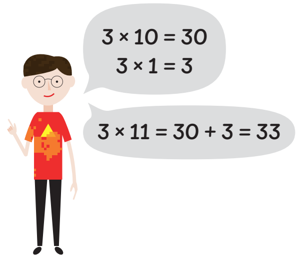
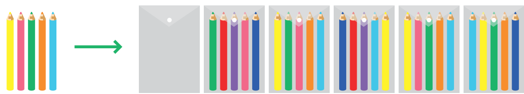
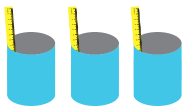
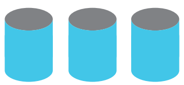
Year	Topic/Strand	Representation	Key Idea
Year 3	**Base 10 Blocks**	Multiply 2 tens by 4.  4 × 2 tens = 8 tens 4 × 20 = 80 	Base 10 blocks are used to support the understanding of multiplication of 2-digit numbers. Language and understanding is developed through the representation of 3 × 20 as 3 × 2 tens = 6 tens. Pupils use known multiplication tables to 10 together with the place–value names of the digits being used to carry out the multiplication.
Year 3	**Number Bonds**	12 × 3 10 2 10 × 3 = 30 2 × 3 = 6	Number bonds are used to show numbers partitioned into tens and ones before being multiplied. The examples being used move from a number bond relating to an equation to an equation and the formal written method.
Year 3	**Formal Written Method**	Step 1 Multiply the ones. 6 ones × 4 = 24 ones 24 ones = 2 tens + 4 ones 2 tens $\begin{array}{rrr} & {}^{2}3 & 6 \\ \times & & 4 \\ \hline & & 4 \end{array}$ 4 ones Step 2 Multiply the tens. 3 tens × 4 = 12 tens 12 tens + 2 tens = 14 tens $\begin{array}{rrr} h & t & o \\ & {}^{2}3 & 6 \\ \times & & 4 \\ \hline 1 & 4 & 4 \end{array}$ 36 × 4 = 144	This method is used to multiply a 2-digit number by a 1-digit number. Initially, the method shows the product of the multiplication of the ones, then the product of the multiplication of the tens, before adding the products to find the total. This method progresses to include renaming and finally moves to a shortened form of the written method. The method is finally shown as a version of the formal written method, in which the product of the multiplication of each place is shown as a single product, with any renaming added above each place in the multiplication.

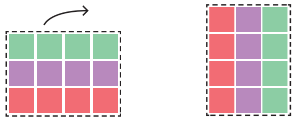
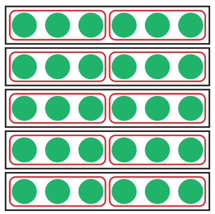
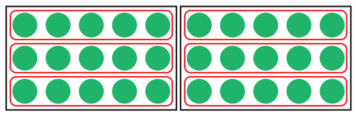
Multiplication Calculation Policy

Year 4

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 4</td><td>Counting in 6s, 7s and 9s</td><td>Count on in sixes.
<table>
<tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr>
<tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr>
<tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr>
</table></td><td>When pupils know that the size of a group is 6, 7 and 9 and the group size remains consistent, they can count in multiples of 6, 7 and 9 to find the product.

Counting in multiples is supported by representation on a number line using intervals of 6, 7 and 9.</td></tr>
<tr><td>Year 4</td><td>Equal Groups</td><td>
4 boxes of 6
4 × 6 = 24</td><td>Multiplication by 6, 7 and 9 is shown initially using equal groups. Specific language is used to support these examples, in this case ‘4 groups of 6’, and this is immediately followed by the equation 4 × 6. This forms the basis of using known facts to find unknown facts.</td></tr>
<tr><td>Year 4</td><td>Number Line</td><td>
</td><td>Counting in multiples is shown on a number line. Multiples of 6, 7 and 9 are used as the intervals on a number line to support skip counting using these multiples. A growing pattern in multiples of 6, 7 and 9 is also shown to support pupils’ understanding.</td></tr>
</table>

Year	Topic/Strand	Representation	Key Idea
Year 4	**Multiplying by 11 and 12 Using Associated Facts**	 10 + 10 + 10 = 30 1 + 1 + 1 = 3  	Learning to multiply by 11 and 12 is supported by partitioning 11 and 12 and using the 10 times table as the basis for initial understanding, building towards immediate recall.
Year 4	**Fact Families**	 30 ÷ 6 = 5 6 × 5 = 30	Fact families are used in the introduction of division, represented using arrays to show the relationship between factors and a product. Pupils relate 6 × 11 = 66 to 66 ÷ 6 = 11. They understand that multiplication can be used in division calculations.
Year 4	**Multiplying by 0 and 1**	 *3 pots of 1 ruler* 3 × 1 = 3  *3 empty pots* 3 × 0 = 0	Pupils initially use their understanding of 'groups of' to understand multiplying by zero. For example, 0 × 4 is read as 'There are zero groups of 4'. Pupils' understanding then moves to read 0 × 4 as zero multiplied 4 times. The language is an extension of what they have already learned about multiplication.

Year	Topic/Strand	Representation	Key Idea
Year 4	**Commutativity**	 3 × 4 4 × 3 $3 \times 4 = 4 \times 3$ 3 × 4 is equal to 4 × 3. $5 \times 2 \times 3 = \boxed{}$ $2 \times 3 \times 5 = \boxed{}$  	Arrays are used to support the understanding of commutativity. Pupils learn the pattern of a × b = b × a. Regardless of the order in which the factors are multiplied, the product remains the same. The commutative property is further developed through the multiplication of 3 numbers. 3 factors are multiplied in different orders and the product remains the same.

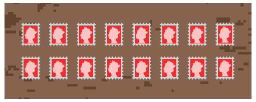
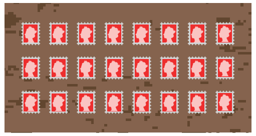
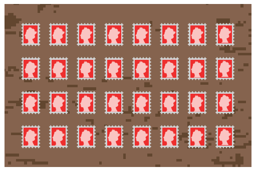
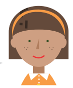
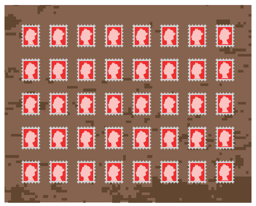
<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 4</td><td>**Multiplying Multiples of 10**</td><td>*30 is equal to 3 tens.*
5 × 3 = 15
5 × 3 tens = 15 tens
= 150
10 10 10
10 10 10
10 10 10
10 10 10
10 10 10
5 × 30 = 150</td><td>Pupils learn to scale a product by a factor of 10 when multiplying a multiple of 10. For example, we know 3 × 4 = 12, therefore the product of 30 × 4 is 10 times greater: 30 × 4 = 120.

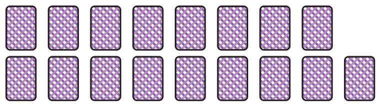
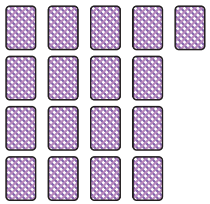
Naming the place value of the digit supports this approach and pupils relate a known fact to multiplying multiples of 10. For example, we can read 30 × 4 as 3 tens × 4. So, 3 tens × 4 = 12 tens or 120.

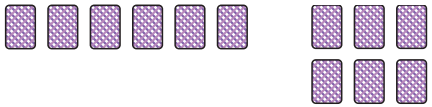
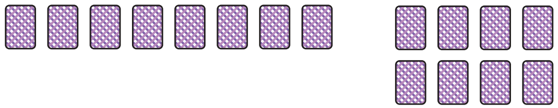
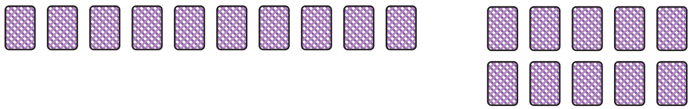
We would expect pupils to generalise and see that 30 × 4 = 3 × 4 × 10. While this isn't formalised, this forms the basis of the distributive property of multiplication.</td></tr>
<tr><td>Year 4</td><td>**Formal Written Method**</td><td>$\begin{array}{rrrrl} & 2 & 1 & 8 & \\ \times & & & 4 & \\ \hline & & 3 & 2 & \longrightarrow 8 \times 4 = 32 \\ & & 4 & 0 & \longrightarrow 10 \times 4 = 40 \\ + & 8 & 0 & 0 & \longrightarrow 200 \times 4 = 800 \\ \hline & 8 & 7 & 2 & \longrightarrow 218 \times 4 = 872 \\ \hline \end{array}$</td><td>Pupils use formal written methods, short and long, to multiply a 2-digit number by a 1-digit number. Initially the long method is used, showing the product of the multiplication of the ones, tens and hundreds, before adding the products to find the total. Pupils are shown the corresponding short formal written method so can make the links between the two procedures. Multiplication then moves from a 2-digit number by a 1-digit number to a 3-digit number by a 1-digit number. Pupils should be aware that even though the number of digits in one number increases, the procedure remains the same.</td></tr>
</table>

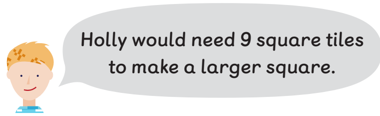
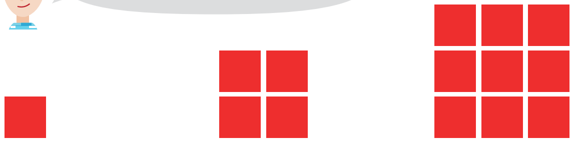
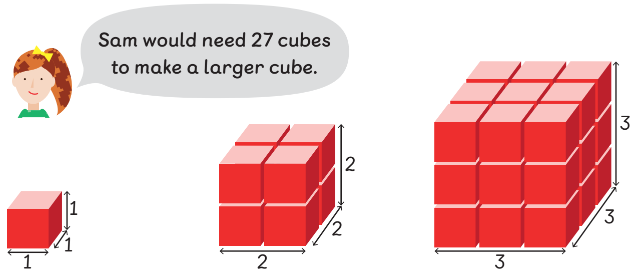
Multiplication Calculation Policy

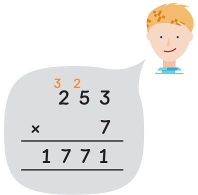
Year 5

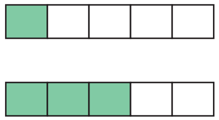
Year	Topic/Strand	Representation	Key Idea
Year 5	Multiples	 1 row of 8 stamps. 1 × 8 = 8  2 rows of 8 stamps. 2 × 8 = 16  3 rows of 8 stamps. 3 × 8 = 24  4 rows of 8 stamps. 4 × 8 = 32 A multiple is a number you get when you multiply one number by another number. 8, 16, 24, 32 and 40 are multiples of 8.   5 rows of 8 stamps. 5 × 8 = 40 The product of 5 and 8 is 40. 40 is a multiple of 5. 40 is also a multiple of 8.  *Sam has 40 stamps altogether.*	Finding multiples is initially related to skip counting. Pupils develop an understanding that counting in 2s produces a series of multiples that are also a product when 2 is a factor. They develop an understanding that the product is the multiple of two numbers.

Year	Topic/Strand	Representation	Key Idea
Year 5	Finding Factors	 2 rows of 12 tiles 2 × 12 = 24  2 and 12 are factors of 24. Factors are the numbers we multiply together to make another number. 2 and 12 are factors of 24 because 2 × 12 = 24.	Pupils have already been working with factors for a significant amount of time but the term 'factors' is introduced in Year 5. The structure for introducing factors uses rectangular arrangements and identifies the number of rows and number of items in each row. Pupils' understanding of factors is further developed when looking at common factors. They learn that different numbers can share some of the same factors. Pupils may go on to generalise about common factors. For example, all integers that end in 0 or 5 have 5 as a common factor.
Year 5	Prime Numbers	 This is a rectangle.  These are not rectangles. There is only one way to arrange 17 cards. 17 = 1 × 17 17 only has two factors, 1 and itself. 17 is a prime number.	Following on from finding factors, pupils use rectangular arrangements to identify a pattern presented by prime numbers. Pupils find that prime numbers can only be arranged in a single rectangular pattern. This leads them to see that certain numbers only have two factors. These numbers, integers greater than 1, are called prime numbers.

Year	Topic/Strand	Representation	Key Idea
Year 5	**Composite Numbers**	 $6 = 1 \times 6$ $6 = 2 \times 3$  $8 = 1 \times 8$ $8 = 2 \times 4$  $10 = 1 \times 10$ $10 = 2 \times 5$ *2 is the only even prime number.* *All other multiples of 2 have more than two factors.*	Once pupils have a sound understanding of multiples, factors and prime numbers, the term 'composite numbers' is used to describe integers, greater than 1, that have more than two factors.

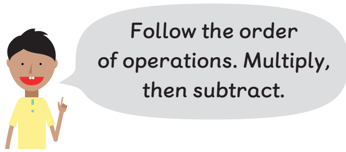
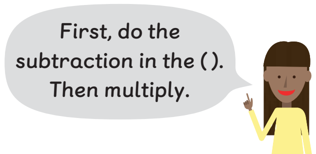
Year	Topic/Strand	Representation	Key Idea
Year 5	**Square and Cube Numbers**	  1 row of 1 $1 \times 1 = 1^2$ $= 1$ 2 rows of 2 $2 \times 2 = 2^2$ $= 4$ 3 rows of 3 $3 \times 3 = 3^2$ $= 9$  $1 \times 1 \times 1 = 1^3$ $= 1$ $2 \times 2 \times 2 = 2^3$ $= 8$ $3 \times 3 \times 3 = 3^3$ $= 27$	Pupils are introduced to both square and cube numbers by the physical representation described by their names. These representations lead to abstraction, with pupils understanding that square numbers are the product of a number multiplied by itself and a cube number is the product made by multiplying a number twice by itself.
Year 5	**Multiplying by 10, 100 and 1000**	$5 \times 1000 = \boxed{}$ 5 × 1 thousand = 5 thousands $5 \times 1000 = 5000$	Pupils build on their understanding of multiplication by factors of 10. They see that when a factor is made 10 times greater, the product is 10 times greater. Pupils use their knowledge of times tables to underpin multiplying by 10, 100 and 1000, so 5 × 1000 is equal to 5 × 1 thousand = 5 thousands or 5000. This follows a pattern that has been introduced in previous years.

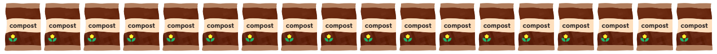
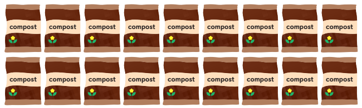
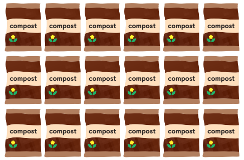
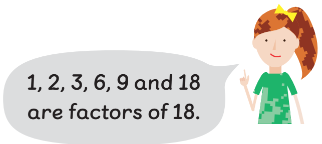
Year	Topic/Strand	Representation	Key Idea
Year 5	**Formal Written Method**	Multiply 253 by 17. $$\begin{array}{r} 2\,5\,3 \\ \times \quad 1\,7 \\ \hline 1\,7\,7\,1 \\ +\ 2\,5\,3\,0 \\ \hline 4\,3\,0\,1 \\ \hline \end{array}$$  	Pupils use formal written methods, short and long, to multiply a 3-digit number by a 1-digit number; then move on to multiply a 4-digit number by a 1-digit number. Initially the long method is used, showing the product as a result of multiplying each place. Pupils then progress to the short formal written method making a link between the two procedures. Next, pupils learn to multiply a 2-digit number by a 2-digit number, then a 3-digit number by a 2-digit number. Links are made to the formal written procedure that they know. Pupils work systematically through the procedure progressing from multiplying by ones to multiplying by tens and ones.

Year	Topic/Strand	Representation	Key Idea
Year 5	**Multiplying Fractions**	$\frac{1}{5}$ $3 \times \frac{1}{5} = \frac{3}{5}$ 	Multiplying a fraction by a whole number is underpinned by the early idea of adding equal groups. Pupils understand that we need to add and multiply items that have the same noun. We read $\frac{1}{5} \times 3$ as 1 fifth × 3 = 3 fifths, in the same was we would read 1 kg × 3 = 3 kg. Bar models are used as pictorial support to show the multiplication of fractions with the same denominator. Pupils progress to multiplying mixed numbers by whole numbers. The approach remains the same but uses partitioning, so pupils multiply the fraction and whole number separately and add the products.

Multiplication Calculation Policy

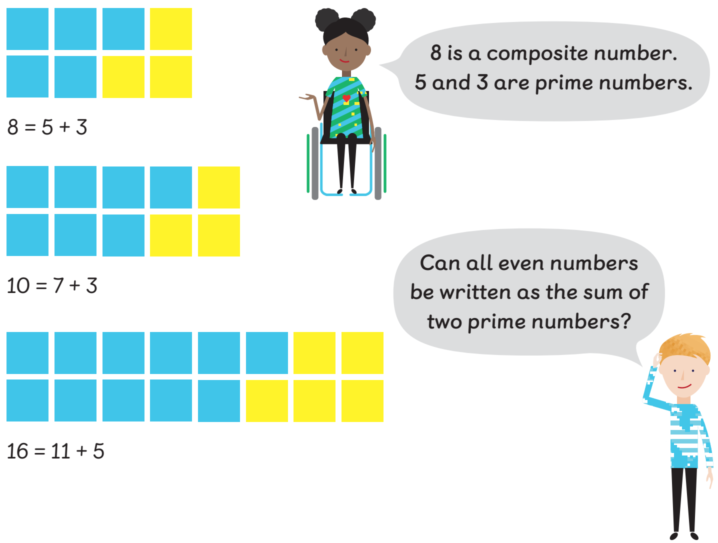
Year 6

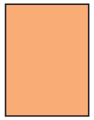
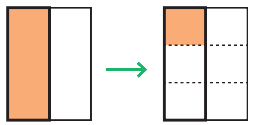
Year	Topic/Strand	Representation	Key Idea
Year 6	**Order of Operations**	*First, carry out all the operations in ( ).* *Next, perform all the multiplication and division.* *Then, calculate all the addition and subtraction.* $15 - 4 \times 3 = 15 - 12 = 3$ $(15 - 4) \times 3 = 11 \times 3 = 33$  	Pupils use the multiplication skills they have learned in previous years within expressions and equations that use multiple operations. Pupils learn to multiply within brackets first, then left to right in expressions and equations that use multiplication. The procedures to multiply remain the same throughout.
Year 6	**Multiplying by 2-Digit Numbers**	£1229 × 28 = ☐ $\begin{array}{cccccc} & & {}^{1}1 & {}^{2}2 & {}^{1,7}2 & 9 \\ \times & & & & 2 & 8 \\ \hline & & 9 & 8 & 3 & 2 \\ + & 2 & 4 & 5 & 8 & 0 \\ \hline & 3 & 4 & 4 & 1 & 2 \end{array}$ → 1229 × 8 = 9832 → 1229 × 20 = 24 580 → 1229 × 28 = 34 412	Pupils revisit the formal written method, multiplying up to 4-digit numbers by 2-digit numbers.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 6</td><td>Common Factors</td><td>
1 row of 18 bags
$1 \times 18 = 18$

2 rows of 9 bags
$2 \times 9 = 18$

3 rows of 6 bags
$3 \times 6 = 18$
</td><td>Prior learning is expanded on by finding common factors within more challenging word problems.

Pupils are encouraged to partition larger numbers into known multiples to determine if the given number is a factor.</td></tr>
<tr><td>Year 6</td><td>Common Multiples</td><td>
<table>
<tr><td>Multiples of 4</td><td>4</td><td>8</td><td>12</td><td>16</td><td>20</td><td>24</td><td>28</td><td>32</td><td>36</td><td>40</td><td>44</td><td>48</td></tr>
<tr><td>Multiples of 6</td><td>6</td><td>12</td><td>18</td><td>24</td><td>30</td><td>36</td><td>42</td><td>48</td><td>54</td><td>60</td><td>66</td><td>72</td></tr>
<tr><td>Multiples of 8</td><td>8</td><td>16</td><td>24</td><td>32</td><td>40</td><td>48</td><td>56</td><td>64</td><td>72</td><td>80</td><td>88</td><td>96</td></tr>
</table>

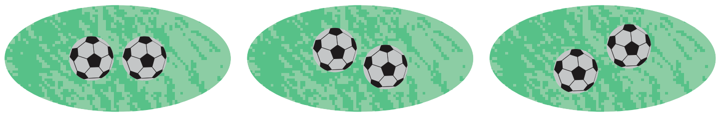
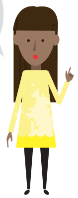
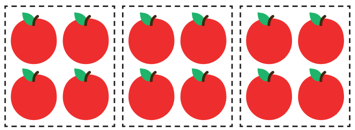
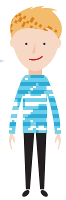
24 and 48 are common multiples of 4, 6 and 8.</td><td>Pupils are introduced to common multiples with the understanding that they are a multiple of 2 or more numbers.</td></tr>
</table>

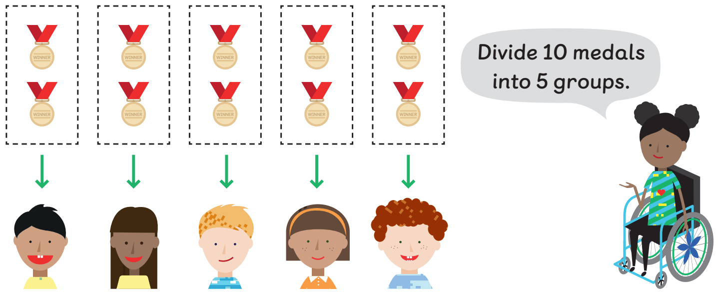
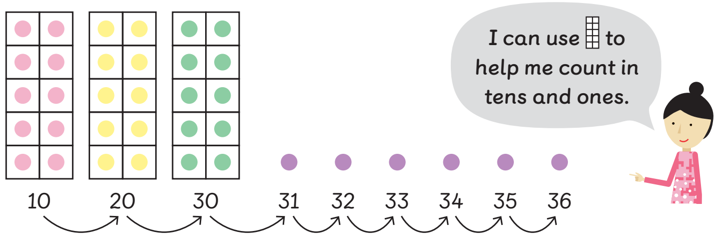
Year	Topic/Strand	Representation	Key Idea
Year 6	Prime Numbers		Pupils' understanding of prime numbers is expanded through the use of Goldbach's conjecture, that all even numbers greater than 2 can be expressed as the sum of two prime numbers.

Year	Topic/Strand	Representation	Key Idea
Year 6	**Multiplying Fractions**	$\frac{1}{3} \times \frac{1}{2}\,l =$  = 1 l of juice  $\frac{1}{2}\,l$ $\frac{1}{3} \times \frac{1}{2}\,l$ $\frac{1}{3}$ of $\frac{1}{2}\,l$ is $\frac{1}{6}\,l$.	Pupils learn to multiply proper fractions by proper fractions. They read fractions to support multiplication, so $\frac{1}{3} \times \frac{1}{5}$ is read as 'What is $\frac{1}{3}$ of $\frac{1}{5}$?' Bar models are used to represent these problems pictorially. Pupils progress to realise that the numerators can be multiplied and the denominators can be multiplied, but before this procedure can be embedded, pupils must have a deep understanding of what the equation means.
Year 6	**Multiplying Decimals**	$\begin{array}{r} {}^{1}7\,.\,{}^{1}2\ 3 \\ \times \qquad 6 \\ \hline 4\ 3\,.\,3\ 8 \\ \hline \end{array}$	Pupils use the same formal written method procedure as they have previously. Pupils need to pay special attention to the places of the digits in the multiplication. It is important that they do not see the decimal point as a place but rather as a symbol used to separate the whole parts from the decimal parts of a mixed number.

Division Calculation Policy

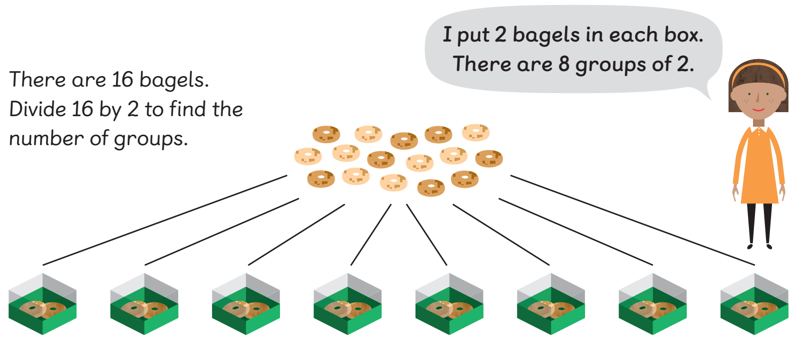
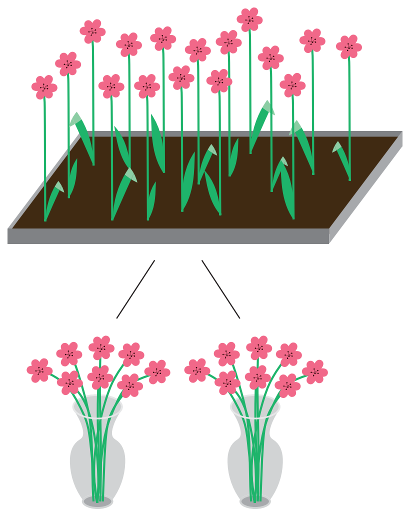
Year 1

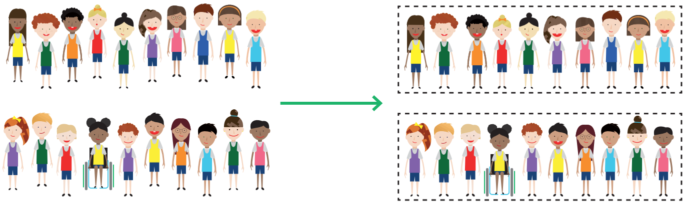
Year	Topic/Strand	Representation	Key Idea
Year 1	Equal Groups	 *There are 2 in each group.* *Each group has an equal number of .* *The balls are in equal groups.* *How many are in each group?* 	Pupils learn to recognise groups that are equal in quantity, initially using like items and then progressing to different items. Pupils understand that equal groups can be represented by concrete items, diagrams and written numbers. Pupils need to be secure in the abstraction principle of counting the quantity of items regardless of the items' properties or characteristics, in order to recognise equal groups in a range of situations.
Year 1	Grouping	*Sam has 12 apples.* *He puts the apples into groups of 4.*  *Each group has an equal number of .*  *How many groups does he make?* *Sam makes groups.*	Pupils initially use grouping for division. They put items into equal groups to find the number of equal groups that can be made from a set amount.

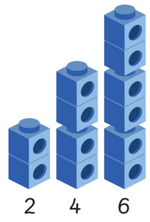
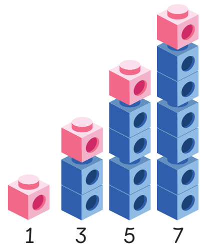
Year	Topic/Strand	Representation	Key Idea
Year 1	Sharing	*10 medals are shared equally among 5 friends.* *How many medals does each friend get?*  Each friend gets 2 medals.	Pupils move from division through grouping to division through sharing. They share a set amount of items equally between a number of groups. The number of groups is known and pupils find the number of items in each group.
Year 1	Counting in 2s, 5s and 10s		Pupils start to count in multiples of 2 and multiples of 10, then progress to counting in multiples of 2, 5 and 10 supported by discrete, countable representations.

Division Calculation Policy

Year 2

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 2</td><td>Grouping</td><td>
</td><td>Pupils initially use grouping for division. They put items into equal groups to find the number of equal groups that can be made from a set amount.</td></tr>
<tr><td>Year 2</td><td>Sharing</td><td>There are 16 flowers.
Elliott cuts the flowers and puts them equally into 2 vases.

There are 8 flowers in each vase.
16 ÷ 2 = 8</td><td>Pupils move from division through grouping to division through sharing. They share a set amount of items equally between a number of groups.
The number of groups is known and pupils find the number of items in each group.</td></tr>
</table>

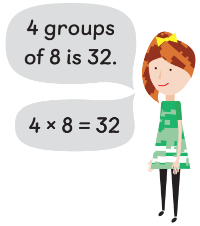
Year	Topic/Strand	Representation	Key Idea
Year 2	Division by 2, 5 and 10	*20 children can be put into teams of 10.*  20 ÷ 10 = 2 *There are 2 equal teams.* There are 2 groups of 10 children. 2 × 10 = 20  10 × 2 = 20 20 ÷ 2 = 10 2 × 10 = 20 20 ÷ 10 = 2 There is a relationship between the multiplication and division facts.  *This is a multiplication and division fact family.*	Pupils start to make the connection between division and multiplication. They see amounts as equal groups and relate this to multiplication.

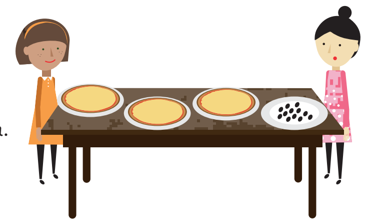
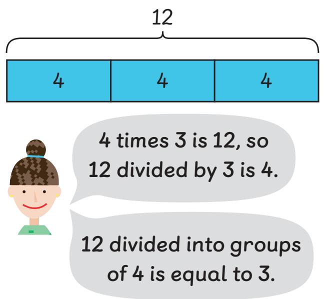
Year	Topic/Strand	Representation	Key Idea
Year 2	Odd and Even Numbers	 2 cubes can be put into a group of 2. 4 cubes can be put into groups of 2. 6 cubes can be put into groups of 2. 2, 4 and 6 are even numbers.  1 cube cannot be put into a group of 2. 3 cubes cannot be put into groups of 2. 5 cubes cannot be put into groups of 2. 7 cubes cannot be put into groups of 2. 1, 3, 5 and 7 are odd numbers.	Pupils develop an understanding that even numbers can be put into groups of 2 exactly. Numbers that can be put into groups of 2 and have 1 remaining are described as odd numbers.

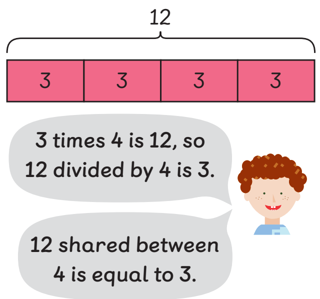
Division Calculation Policy

Year 3

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 3</td><td>Dividing by 3, 4 and 8</td><td>Sam put 32 cobs of corn into 4 equal groups.

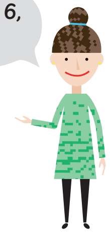
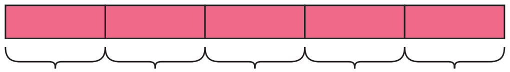


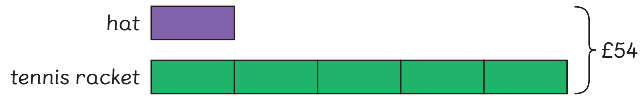
32 ÷ 4 = 8
Each group has 8 cobs of corn.</td><td>Pupils are introduced to the division of numbers by 3, 4 and 8 using grouping initially. They make groups of 3, 4 and 8 and then move on to sharing a total.</td></tr>
<tr><td>Year 3</td><td>Division within Word Problems</td><td>Amira and Ruby are making pizzas.
They have 12 olives.
They want to put 3 or 4 olives on each pizza.
Can we make a family of multiplication and division equations to help them?



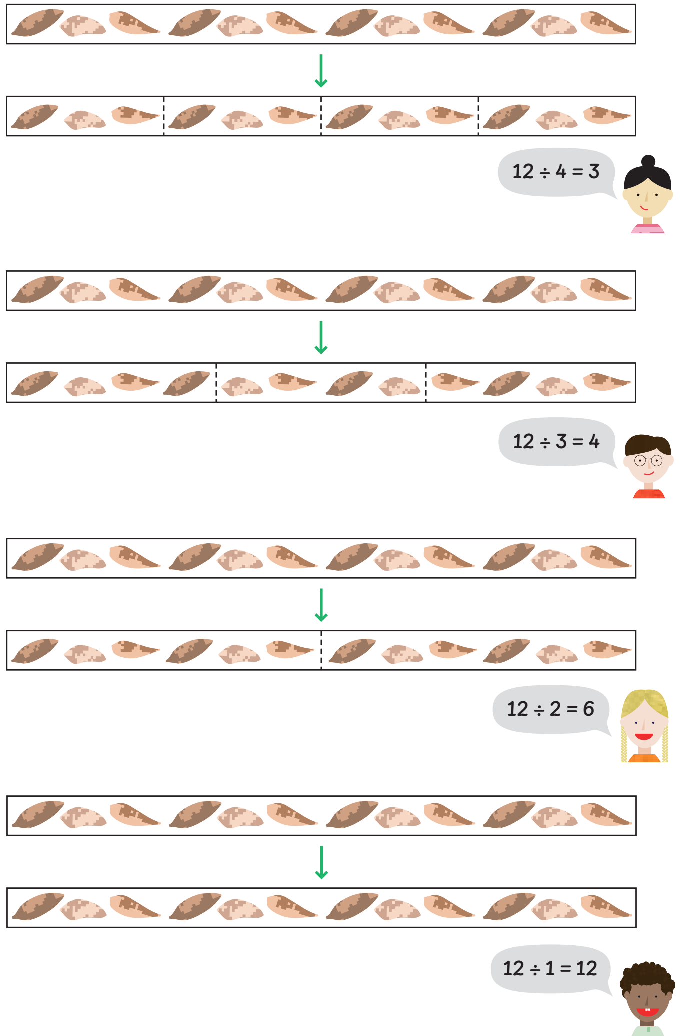

</td><td>Pupils extend their understanding of division by relating the division facts to multiplication facts, creating a multiplication and division fact family. Word problems get increasingly more complex and bar models are used to represent problems involving division.</td></tr>
</table>

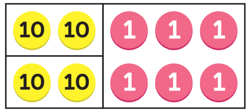
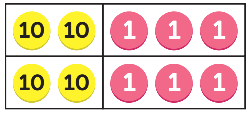
Division Calculation Policy

Year 4

Year	Topic/Strand	Representation	Key Idea
Year 4	**Dividing by 6, 7 and 9**	 $30 \div 6 = 5$ $6 \times 5 = 30$ *Each packet can hold 5 pencils.* When 30 is divided by 6, **the quotient** is 5. 	Pupils are given division word problems and immediately relate the division used to solve the problem to the multiplication fact they have previously learned. The language associated with division is given, with pupils understanding that when the number is divided, the outcome is called the quotient.
Year 4	**Dividing by 11 and 12**	 12 12 12 12 12 $5 \times 12 = \square$ $\square \div 12 = \square$ $12 \times 5 = \square$ $\square \div 5 = \square$	Arrays and bar models are used to show the relationship between multiplication and division when learning to multiply and divide by 11 and 12, building on the relationship already learned when dividing by 6, 7 and 9.

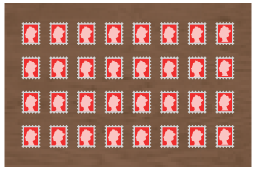
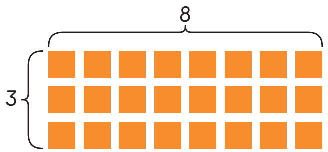
Year	Topic/Strand	Representation	Key Idea
Year 4	**Dividing with Remainders**	There are 13 flowers.  13 ÷ 3 = 4 with 1 left over The quotient is 4. The remainder is 1.	Pupils learn that when dividing into equal groups, we can be left with a number of items less than the group size. This is introduced as the remainder. Initially, the remainder is shown as a whole number.
Year 4	**Word Problems Involving Division**	 6 units → £54 1 unit → £54 ÷ 6 = £9	Division word problems are supported by the use of arrays and bar models, reinforcing the idea of equal groups. Pupils relate the representations of the problems to the equations given. Comparison division models are also used to determine amounts when two separate amounts are compared.

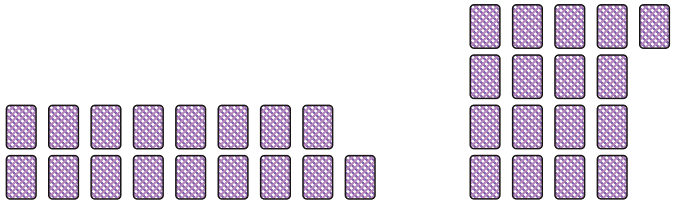
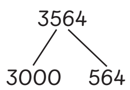
Year	Topic/Strand	Representation	Key Idea
Year 4	Dividing by 1		Pupils look for a pattern and generalise about dividing by 1. They systematically work through dividing a single amount by 4, 3, 2 and finally 1 to make observations about the number of groups and the size of each group.

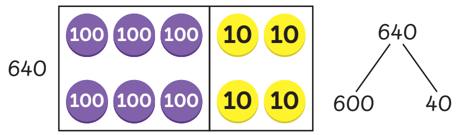
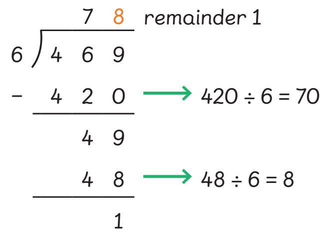
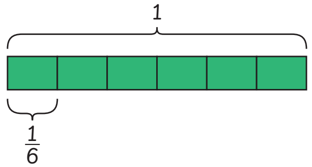
Year	Topic/Strand	Representation	Key Idea
Year 4	**Dividing 2-Digit Numbers**	*Step 1* Divide 4 tens by 2.  4 tens ÷ 2 = 2 tens 40 ÷ 2 = 20 $\boxed{20}$ $\begin{array}{r} 2 \\ 2\overline{)46} \\ -40 \end{array}$ *Step 2* Divide 6 ones by 2.  6 ones ÷ 2 = 3 ones 6 ÷ 2 = 3 46 ÷ 2 = 23 $\begin{array}{r} 23 \\ 2\overline{)46} \\ -40 \\ \hline 6 \\ 6 \\ \hline 0 \end{array}$	Pupils initially use place–value counters to support the division of 2-digit numbers, then move on to use a long formal written method. The long written method shows the systematic division of parts of the dividend resulting in the quotient.
Year 4	**Dividing 3-Digit Numbers**	306 ÷ 3 = 	The same procedure used for dividing 2-digit numbers is used for dividing 3-digit numbers. Place–value counters are used to represent the problem before moving on to use the long formal written method.

Division Calculation Policy

Year 5

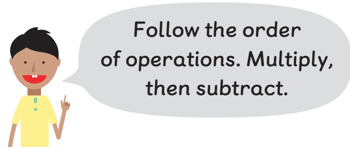
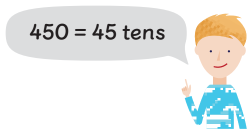
Year	Topic/Strand	Representation	Key Idea
Year 5	Finding Multiples	 4 rows of 8 stamps. 4 × 8 = 32 A multiple is a number you get when you multiply one number by another number. 8, 16, 24, 32 and 40 are multiples of 8. 	Pupils use arrays to recognise multiples as the total number once a number is multiplied by another number. Skip counting is related to multiples as it is shown on a number line. Pupils also look for patterns when identifying multiples on number squares.
Year 5	Finding Factors	 3 rows of 8 tiles 3 × 8 = 24 3 and 8 are factors of 24. 	The same rectangular arrangement that was used to find multiples is used to identify factors. The pictorial representation leads to an understanding that factors are the numbers we multiply to produce a product.
Year 5	Find Common Factors	Factors of 10: 1, 2, 5, 10 Factors of 15: 1, 3, 5, 15	Pupils learn that when multiple numbers share the same factors, we can describe those factors as common factors. Pupils will begin to generalise about common factors. For example, all whole numbers ending in zero will have 5 as a multiple.

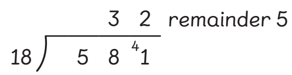
Year	Topic/Strand	Representation	Key Idea
Year 5	**Prime and Composite Numbers**	 *This is a rectangle.*  *These are not rectangles.* *There is only one way to arrange 17 cards.* *17 = 1 × 17* *17 only has two factors, 1 and itself. 17 is a prime number.*	Pupils use their understanding of rectangular arrays to look for prime numbers. They learn that any number that can only be made into a single rectangular array is a prime number. In describing this array, they make the connection that prime numbers only ever have two factors, itself and 1. They also learn that numbers with two or more factors can be described as composite numbers.
Year 5	**Dividing by 10, 100 and 1000**	*How many groups of 1000 can we make from 3564?*    	Place–value counters and numbers bonds are initially used to represent division problems involving dividing by 10, 100 and 1000. Pupils use their understanding of place value to support the division calculations. For example, 35 hundreds ÷ 1 hundred = 35.

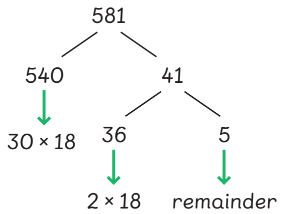
Year	Topic/Strand	Representation	Key Idea
Year 5	**Dividing without Remainder**		Pupils use place–value counters and number bond diagrams to support their understanding of the long formal written method for division. Pupils are shown how numbers can be partitioned into known multiples before carrying out the division.
Year 5	**Dividing with Remainder**	  $1 \div 6 = \frac{1}{6}$ $469 \div 6 = 78\frac{1}{6}$	The same procedure used for dividing without a remainder is used for dividing with a remainder but once pupils have made the maximum possible number of equal groups, they have a quantity remaining that is less than the equal group size. This is the remainder. Initially, the remainder is shown as a whole number. This progresses to showing the remainder as a fraction. This progression is supported pictorially with a bar model. Pupils should also start to become aware that the representation of the remainder will be determined by the context of the problem.

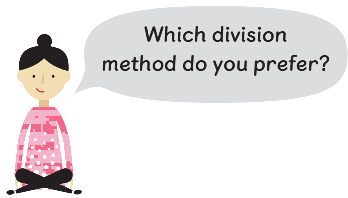
Division Calculation Policy

Year 6

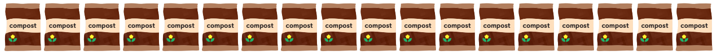
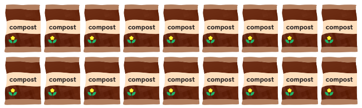
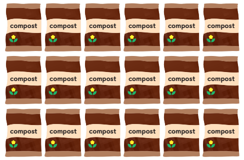
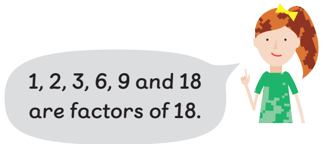
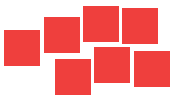
Year	Topic/Strand	Representation	Key Idea
Year 6	**Order of Operations**	$15 - 4 \times 3 = 15 - 12$ $= 3$  	Pupils understand the order to calculate expressions and equations that have multiple operations.
Year 6	**Dividing by a 2-Digit Number without Remainder**	$450 \div 15 = \boxed{}$ 45 tens ÷ 15 = 3 tens 450 ÷ 15 = 30  	Pupils use simple division to help them calculate more complex division. Initially, pupils understand that if the dividend increases by a factor of 10 and the divisor remains the same, the quotient will also increase by a factor of 10. So, if 45 ÷ 15 = 3, then 450 ÷ 15 = 30. Pupils also use their understanding of factors to divide. They progress to show division using a long formal written method. Once the long method is understood, pupils move on to divide using a short formal written method. While the process remains the same, the notation changes to keep it within the short division structure.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 6</td><td>Dividing by a 2-Digit Number with Remainder</td><td>

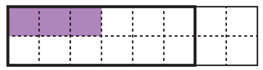



</td><td>The process used when dividing by a 2-digit number without a remainder stays the same when dividing with remainders. The process results in remainders that cannot be put into the equal group size as whole numbers. The context of the problem suggests the form that the remainder will take and pupils decide on the best representation for the remainder depending on the context.

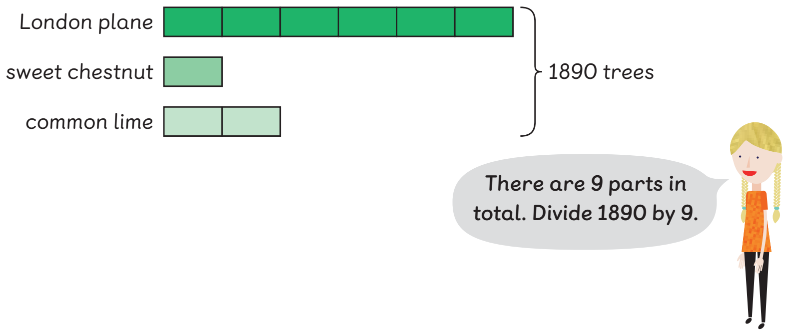
Pupils also use a unitary method of division to solve more complex word problems. Within these problems, they also use brackets to show the partitioning of numbers and how this can be used to support calculation in division problems.</td></tr>
<tr><td>Year 6</td><td>Common Multiples</td><td><table>
<tr><td>Multiples of 4</td><td>4</td><td>8</td><td>12</td><td>16</td><td>20</td><td>24</td><td>28</td><td>32</td><td>36</td><td>40</td><td>44</td><td>48</td></tr>
<tr><td>Multiples of 6</td><td>6</td><td>12</td><td>18</td><td>24</td><td>30</td><td>36</td><td>42</td><td>48</td><td>54</td><td>60</td><td>66</td><td>72</td></tr>
<tr><td>Multiples of 8</td><td>8</td><td>16</td><td>24</td><td>32</td><td>40</td><td>48</td><td>56</td><td>64</td><td>72</td><td>80</td><td>88</td><td>96</td></tr>
</table></td><td>Pupils work systematically through problems looking for common multiples of given numbers.</td></tr>
</table>

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 6</td><td>Common Factors</td><td>
1 row of 18 bags
1 × 18 = 18

2 rows of 9 bags
2 × 9 = 18

3 rows of 6 bags
3 × 6 = 18
</td><td>Pupils use long division to find common factors of given numbers. The method used to find common factors progresses to arrays and using tables to systematically find possible common factors.</td></tr>
<tr><td>Year 6</td><td>Prime Numbers</td><td>Elliott has 7 square tiles.

Elliott can only make 1 rectangular arrangement.

1 row of 7
1 × 7 = 7
The factors of 7 are 1 and 7.
7 is a prime number.</td><td>Arrays are used as they have been previously, looking for rectangular patterns. Pupils see that numbers that can only be made into 1 rectangular arrangement are prime numbers with factors of itself and 1.</td></tr>
</table>

Year	Topic/Strand	Representation	Key Idea
Year 6	**Dividing Fractions by Whole Numbers**	$\frac{3}{4} \div 4 = \square$  $\frac{3}{4} \div 4 = \frac{1}{4} \times \frac{3}{4} = \frac{3}{16}$	Pupils relate dividing fractions by a whole number to multiplying by its reciprocal. So, dividing by 4 is related to multiplying by $\frac{1}{4}$. We also read this as '$\frac{1}{4}$ of'. The procedure of dividing fractions by whole numbers is supported by the use of bar models and pictorial representation.
Year 6	**Dividing Decimals without Renaming**	$\begin{array}{rl} \square . \square\square & \\ 2\overline{)\,8 . 4\ 2} & \\ -\ 8 & \longrightarrow 2 \times 4 \\ \hline 0 . 4 & \\ -\ 0 . 4 & \longrightarrow 2 \times 0.2 \\ \hline 0 . 0\ 2 & \\ -\ 0 . 0\ 2 & \longrightarrow 2 \times 0.01 \\ \hline 0 & \end{array}$	Initially, place–value counters are used to show the division procedure that should be well known by pupils at this stage. The long formal written method is then used to divide decimal numbers without renaming the dividend. The procedure for long division does not change. Pupils need to be mindful of the placement of the digits and remember that the decimal point does not represent a place. Simply, the decimal point separates the whole and fractional parts of a number.

Year	Topic/Strand	Representation	Key Idea
Year 6	**Dividing Decimals with Renaming**	6.15 6 ones, 1 tenth, 5 hundredths 5 ones, 11 tenths, 5 hundredths 5 ones, 10 tenths, 15 hundredths ÷ 5, ÷ 5, ÷ 5 1 one, 2 tenths, 3 hundredths 6.15 ÷ 5 = 1.23	Initially, place–value counters are used to show the division procedure that should be well known by pupils at this stage. The long formal written method is then used to divide decimal numbers without a remainder. The procedure for long division with renaming does not change from what pupils have experienced previously. Pupils need to be mindful of the placement of the digits and remember that the decimal point does not represent a place. Simply, the decimal point separates the whole and fractional parts of a number.
Year 6	**Dividing Decimals by a 2-Digit Whole Number**	4.65 kg ÷ 15 = 4.65 4.5 = 45 tenths ÷ 15 = 3 tenths 0.15 = 15 hundredths ÷ 15 = 1 hundredth 3 tenths + 1 hundredth = 0.3 + 0.01 = 0.31 4.65 ÷ 15 = 0.31	Pupils initially divide decimal numbers by 2-digit whole numbers where the dividend is easily broken into multiples of the divisor. Number bonds demonstrate the partitioning in order to divide using long and short formal written methods of division.

<table>
<tr><th>Year</th><th>Topic/Strand</th><th>Representation</th><th>Key Idea</th></tr>
<tr><td>Year 6</td><td>Ratio</td><td>
</td><td>Pupils use a unitary method involving division to determine quantities in ratio problems. This approach is supported by the use of bar models.</td></tr>
<tr><td>Year 6</td><td>Algebra</td><td><table><tr><td>x</td><td>18</td><td>3</td><td>90</td></tr><tr><td>$\frac{x}{3}$</td><td></td><td></td><td></td></tr></table></td><td>Pupils use their understanding of division to determine unknown values with algebraic expressions and equations.</td></tr>
</table>